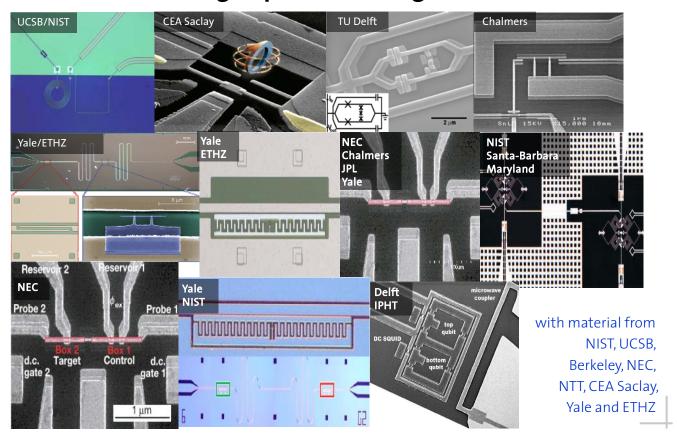
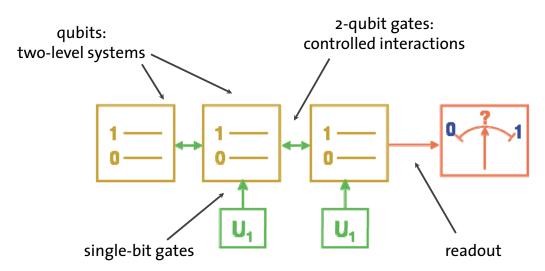
Building a Quantum Information Processor using Superconducting Circuits



Generic Quantum Information Processor

The challenge:



- Quantum information processing requires excellent qubits, gates, ...
- Conflicting requirements: good isolation from environment while maintaining good addressability



The DiVincenzo Criteria

for Implementing a Quantum Computer in the standard (circuit approach) to quantum information processing (QIP):

- #1. A scalable physical system with well-characterized qubits.
- #2. The ability to initialize the state of the qubits.
- #3. Long (relative) decoherence times, much longer than the gate-operation time.
- #4. A universal set of quantum gates.
- #5. A qubit-specific measurement capability.

plus two criteria requiring the possibility to transmit information:

- #6. The ability to interconvert stationary and mobile (or flying) qubits.
- #7. The ability to faithfully transmit flying qubits between specified locations.



Topics

- realization of superconducting quantum electronic circuits
 - harmonic oscillators (photons)
 - non-harmonic oscillators (qubits)
- controlled qubit/photon interactions
 - cavity quantum electrodynamics with circuits
- · qubit read-out
- single qubit control
- decoherence
- two-qubit interactions
 - generation of entanglement
 - · realization of quantum algorithms



Conventional Electronic Circuits

basic circuit elements:



W

basis of modern information and communication technology



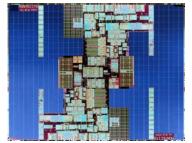
properties:

- classical physics
- no quantum mechanics
- no superposition principle
- no quantization of fields

Eidgenössische Technische Hochschule Zürich Swiss Federal Institute of Technology Zurich first transistor at Bell Labs (1947)



intel dual core processor (2006)

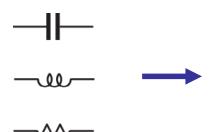


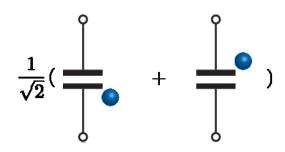
2.000.000.000 transistors smallest feature size 65 nm clock speed ~ 2 GHz power consumption 10 W

Classical and Quantum Electronic Circuit Elements

basic circuit elements:

charge on a capacitor:

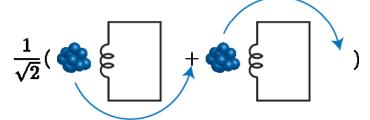




current or magnetic flux in an inductor:

quantum superposition states:

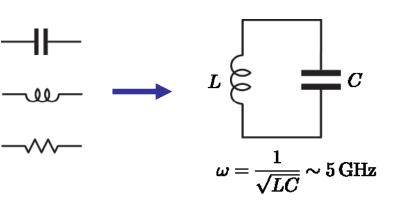
- charge q
- flux o



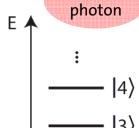
Constructing Linear Quantum Electronic Circuits

harmonic LC oscillator:

basic circuit elements:



energy:



electronic

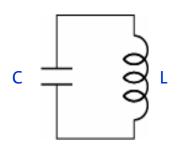
ETH

Eidgenössische Technische Hochschule Zürich

Review: M. H. Devoret, A. Wallraff and J. M. Martinis, condmat/0411172 (2004)

Superconducting Harmonic Oscillator

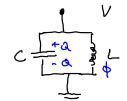
a simple electronic circuit:



- typical inductor: L = 1 nH
- a wire in vacuum has inductance ~ 1 nH/mm
- typical capacitor: C = 1 pF
- a capacitor with plate size 10 μ m x 10 μ m and dielectric AlOx (ϵ = 10) of thickness 10 nm has a capacitance C ~ 1 pF
- resonance frequency

Quantization of the electrical LC harmonic oscillator:

parallel LC oscillator circuit:



voltage across the oscillator:
$$V = \frac{Q}{C} = -L \frac{\partial I}{\partial t}$$

total energy (Hamiltonian):

$$H = \frac{1}{2} CV^2 + \frac{1}{2} LT^2 = \frac{1}{2} \frac{Q^2}{C} + \frac{1}{2} \frac{\varphi^2}{L}$$

with the charge a stored on the capacitor a flux ϕ stored in the inductor

$$Q = VC$$

properties of Hamiltonian written in variables Q and ϕ :

$$\frac{\partial Q}{\partial H} = \frac{C}{C} = -L \frac{\partial L}{\partial L} = -\phi$$

$$\frac{\partial H}{\partial \phi} = \frac{\phi}{L} = I = \hat{Q}$$

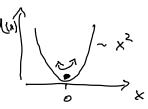
Q and ϕ are canonical variables

see e.g.: Goldstein, Classical Mechanics, Chapter 8, Hamilton Equations of Motion

Quantum version of Hamiltonian

$$\hat{H} = \frac{\hat{Q}^2}{2C} + \frac{\hat{\varphi}^2}{2L}$$

with commutation relation



compare with particle in a harmonic potential:

$$H = \frac{\hat{p}^2}{2m} + \frac{1}{2}m\omega^2 \hat{x}^2$$

analogy with electrical oscillator:

- [\$, \$] [\$, -it =] it
- charge a corresponds to momentum p
- [\$, &] = [\$, -it =] = it

- flux
$$\phi$$
 corresponds to position x

Hamiltonian in terms of raising and lowering operators:

with oscillator resonance frequency:

Raísing and lowering operators:

$$a^{\dagger}(n) = \sqrt{m+1}(n+1)$$
; $\hat{a}(n) = \sqrt{m}(m-1)$
 $a^{\dagger}a(n) = m(n)$ number operator

in terms of α and ϕ :

$$\hat{a} = \frac{1}{\sqrt{2t+2}} \left(2 \hat{Q} + i \hat{\phi} \right)$$

with Ze being the characteristic impedance of the oscillator

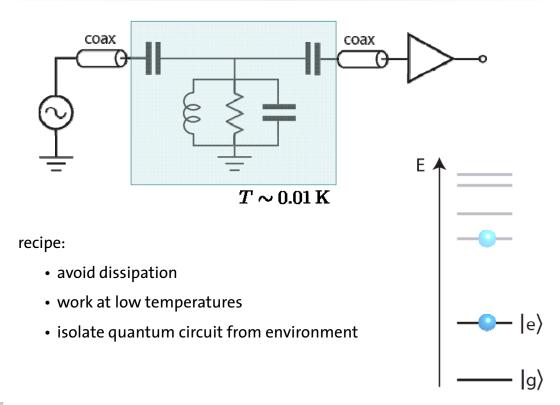
$$2_{c} = \sqrt{\frac{L}{c}}$$

charge \mathbf{Q} and flux $\mathbf{\varphi}$ operators can be expressed in terms of raising and lowering operators:

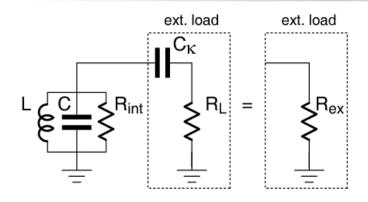
Exercise: Making use of the commutation relations for the charge and flux operators, show that the harmonic oscillator Hamiltonian in terms of the raising and lowering operators is identical to the one in terms of charge and flux operators.

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How to Operate Circuits Quantum Mechanically?



Internal and External Dissipation in an LC Oscillator



internal losses: $R_{
m int}$ conductor, dielectric

external losses: $R_{
m ext}$ radiation, coupling

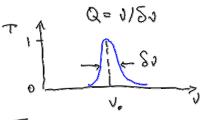
total losses

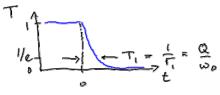
$$\frac{1}{R} = \frac{1}{R_{\text{int}}} + \frac{1}{R_{\text{out}}}$$

$$Z = \sqrt{\frac{L}{C}}$$

$$Q = \frac{R}{Z} = \omega_0 RC$$

$$\Gamma_1 = \frac{\omega_0}{Q} = \frac{1}{RC}$$

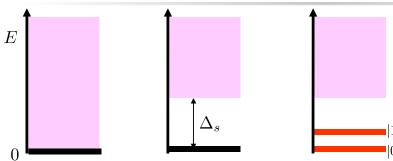




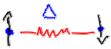
problem 2: internal and external dissipation

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Why Superconductors?



Cooper pairs: bound electron pairs



Bosons (S=o, L=o)

normal metal

superconductor

How to make qubit?

- single non-degenerate macroscopic ground state
- elimination of low-energy excitations

Superconducting materials (for electronics):

- Niobium (Nb): $2\Delta/h = 725 \text{ GHz}$, $T_c = 9.2 \text{ K}$
- Aluminum (AI): $2\Delta/h = 100 \text{ GHz}$, $T_c = 1.2 \text{ K}$

2 chunks of superconductors





macroscopic wave function

Cooper pair density \textbf{n}_i and global phase δ_i



phase quantization: $\delta = \kappa 2 \pi$ flux quantization: $\phi = \kappa \phi_0$

