



Quantum computing with trapped ions



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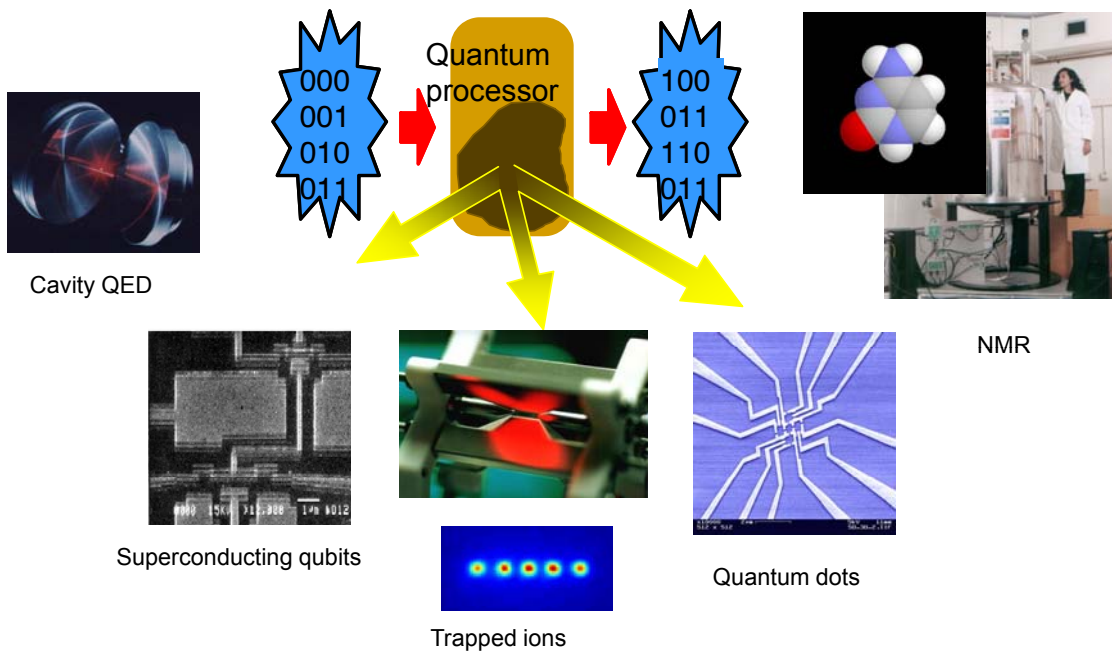
- Basics of ion trap quantum computing
- Measuring a density matrix
- Quantum gates

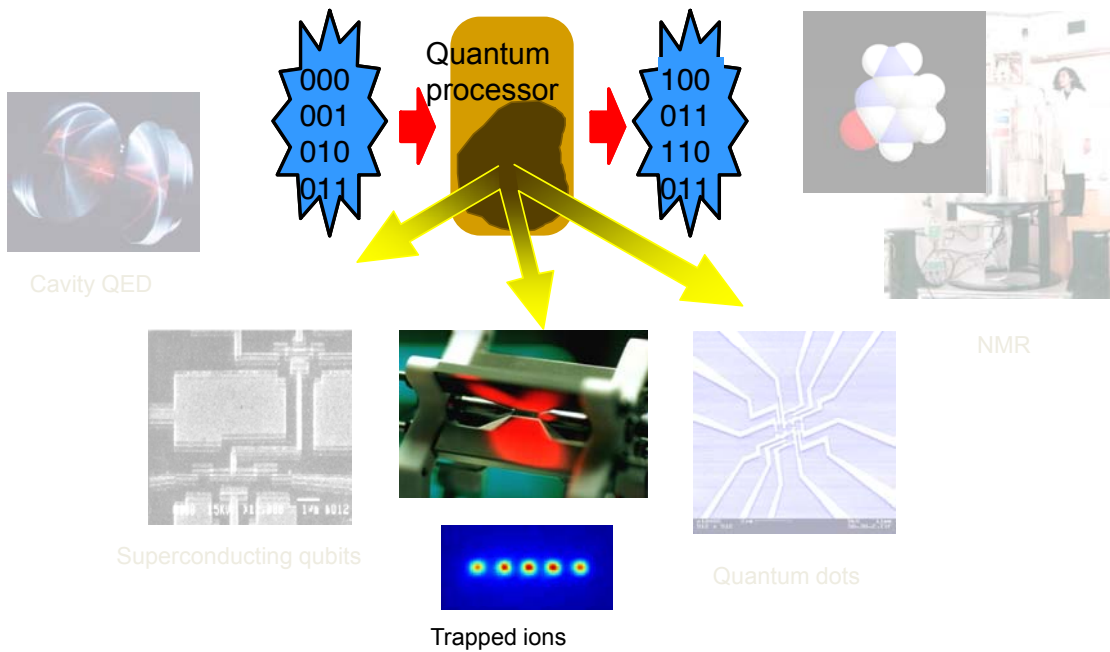


Zürich, Dec 8th 2008



Which technology ?





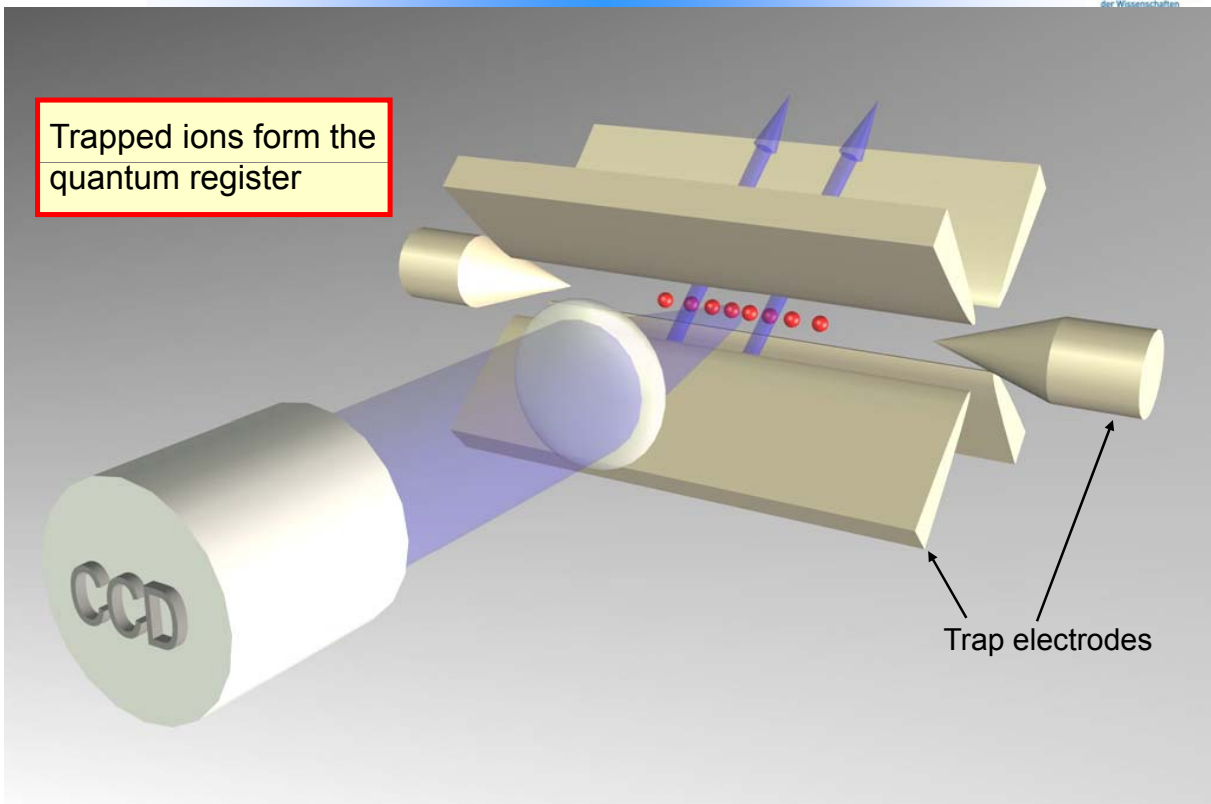
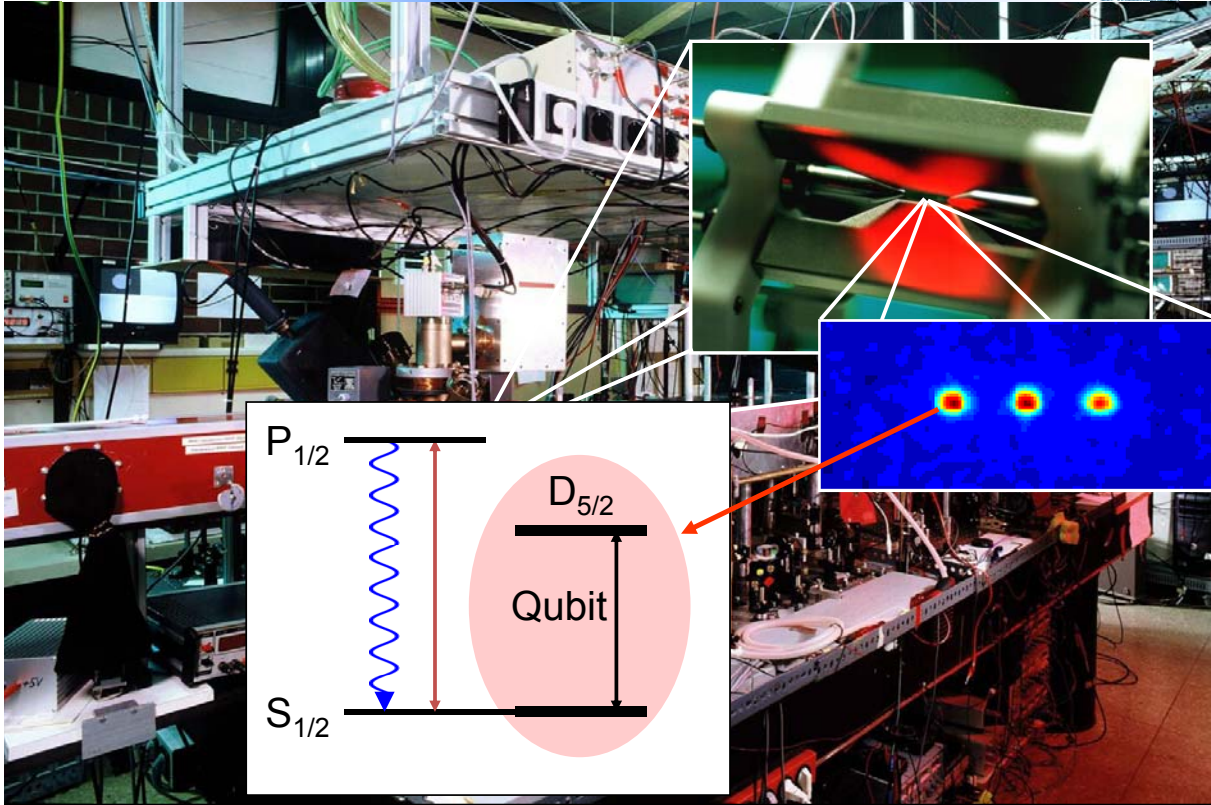
© A. Ekert

Good things about ion traps:

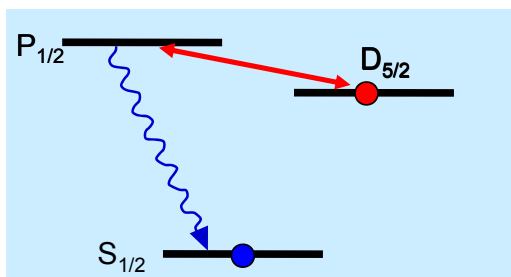
- Ions are excellent quantum memories; single qubit coherence times > 10 minutes have been demonstrated
- Ions can be controlled very well
- Many ideas to scale ion traps

Bad things about ion traps:

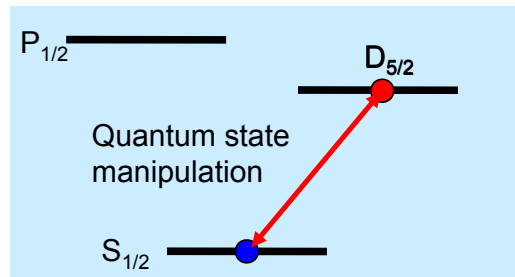
- Slow (~1 MHz)
- Technically demanding



- I. Scalable physical system, well characterized qubits
- II. Ability to initialize the state of the qubits
- III. Long relevant coherence times, much longer than gate operation time
- IV. “Universal” set of quantum gates
- V. Qubit-specific measurement capability

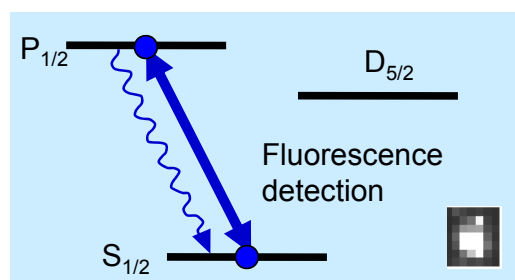


1. Initialization in a pure quantum state



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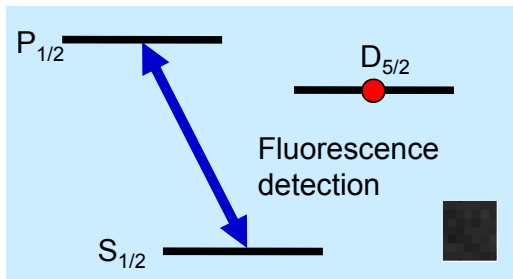
2. Quantum state manipulation on $S_{1/2} - D_{5/2}$ transition



1. Initialization in a pure quantum state:

2. Quantum state manipulation on $S_{1/2} - D_{5/2}$ transition

3. Quantum state measurement by fluorescence detection



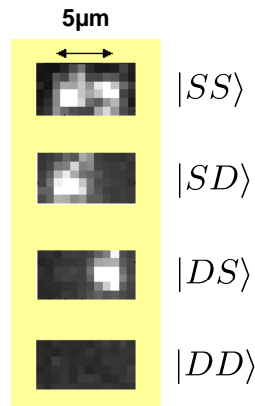
1. Initialization in a pure quantum state:

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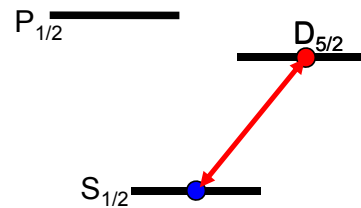
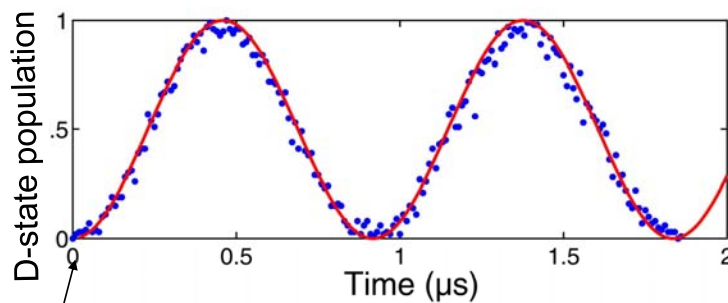
Two ions:

Spatially resolved detection with CCD camera



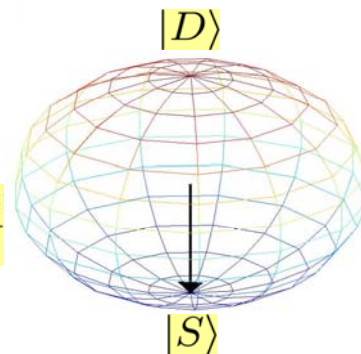
50 experiments / s

Repeat experiments 100-200 times

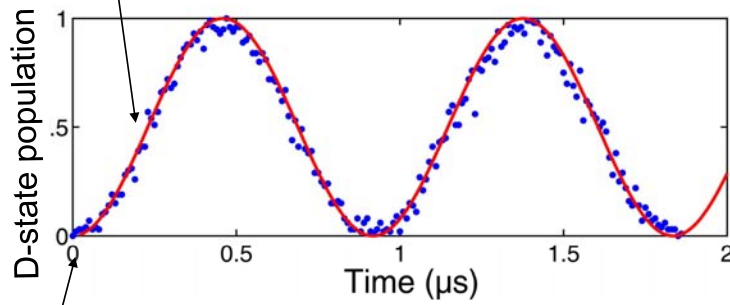
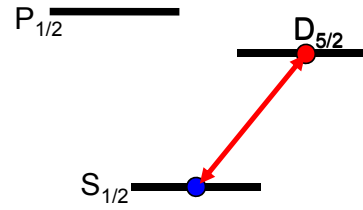


$|S\rangle$

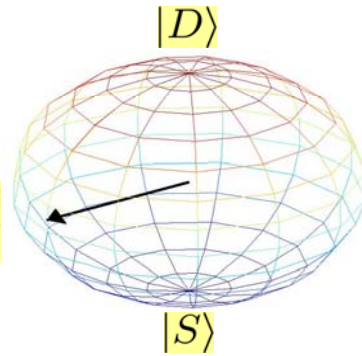
$$\frac{|S\rangle + |D\rangle}{\sqrt{2}}$$



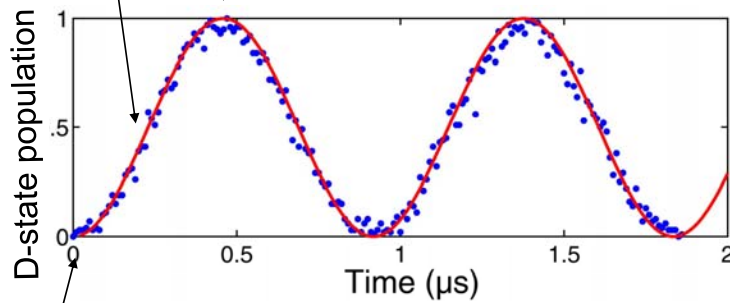
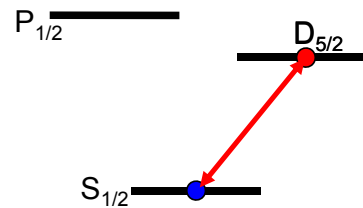
$$\frac{|S\rangle + |D\rangle}{\sqrt{2}}$$


 $|S\rangle$


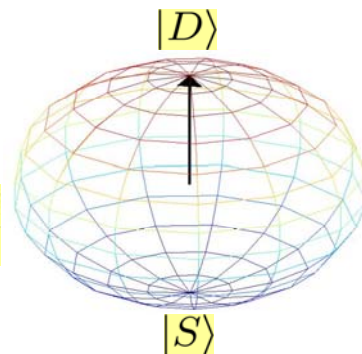
$$\frac{|S\rangle + |D\rangle}{\sqrt{2}}$$

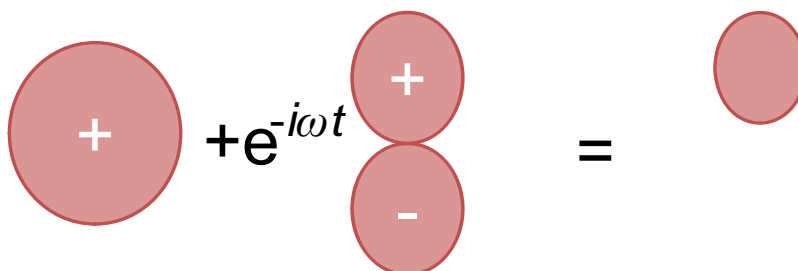
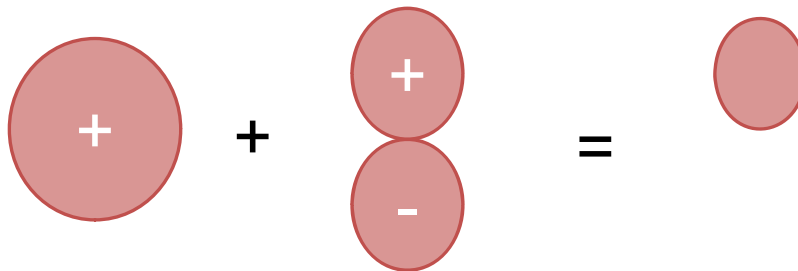
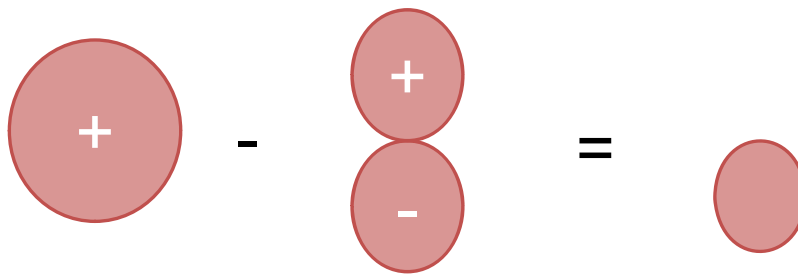
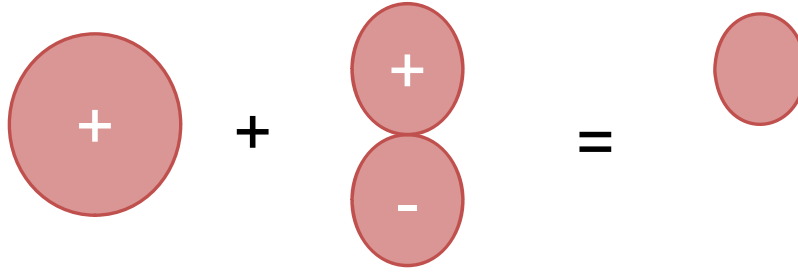


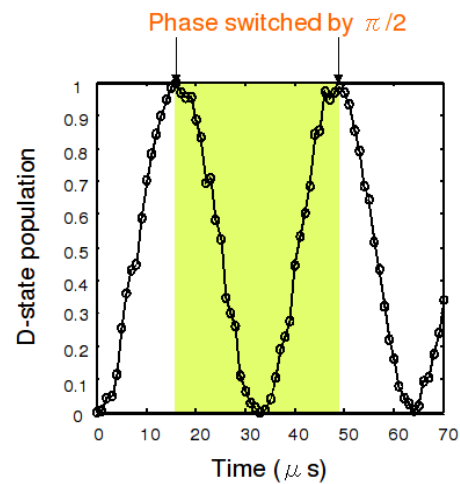
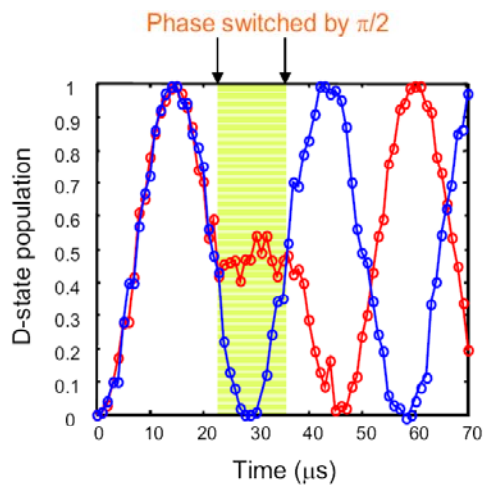
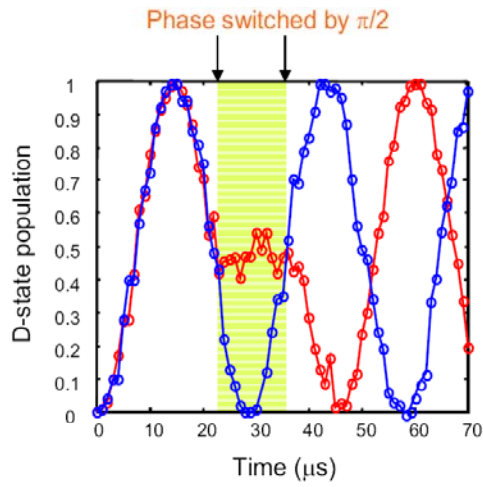
$$\frac{|S\rangle + |D\rangle}{\sqrt{2}}$$

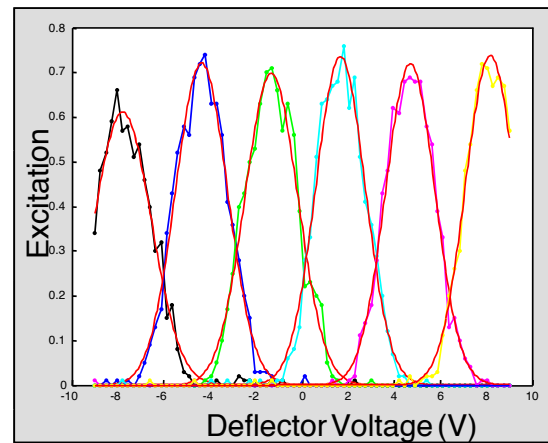
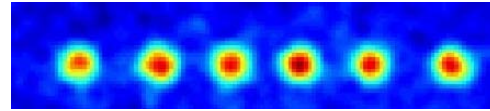
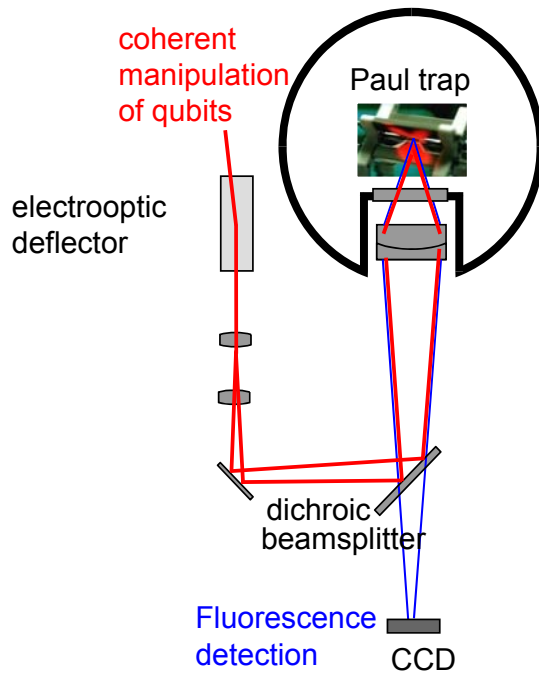

 $|S\rangle$


$$\frac{|S\rangle + |D\rangle}{\sqrt{2}}$$









- inter ion distance: $\sim 4 \mu\text{m}$
- addressing waist: $\sim 2 \mu\text{m}$
- < 0.1% intensity on neighbouring ions

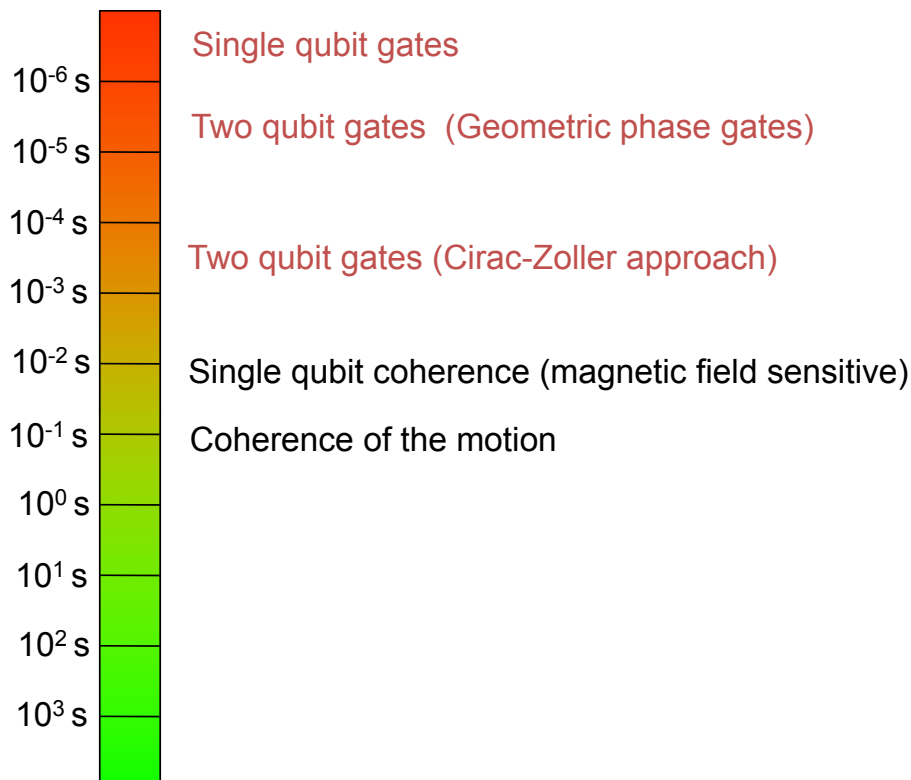
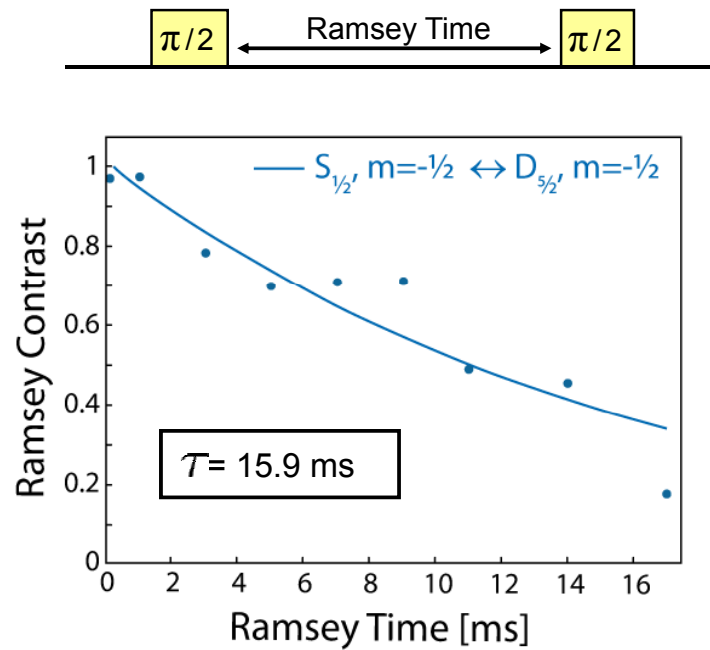
Memory errors:

- Bit-flips
- Dephasing

Operational errors

- technical imperfections ...

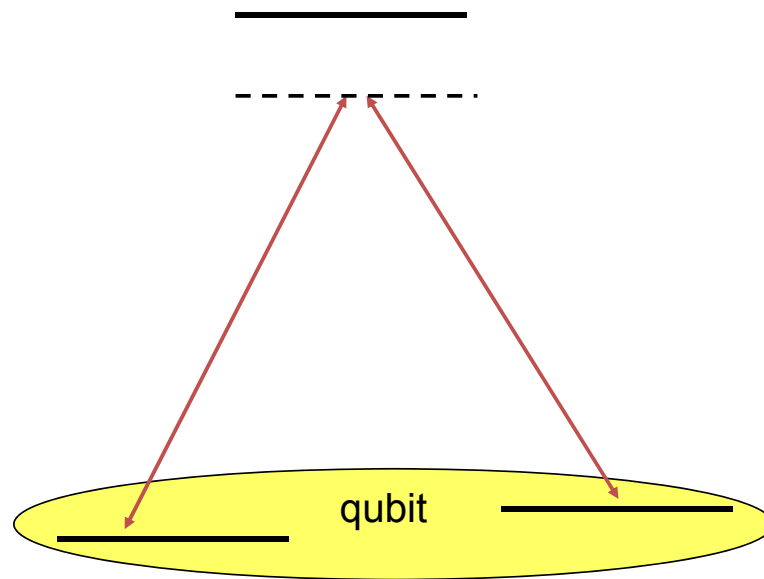
Ramsey Experiment



Raman transitions:

Excited state

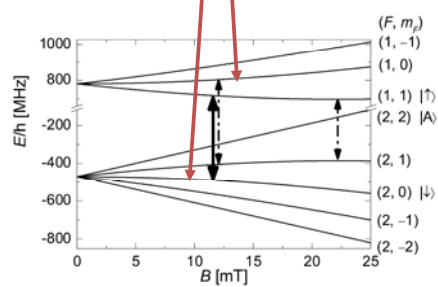
Ground state

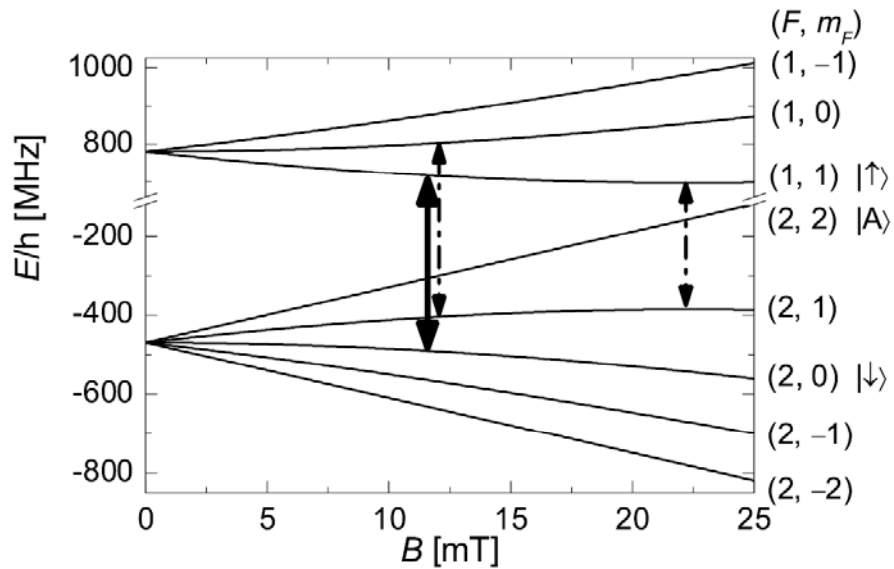
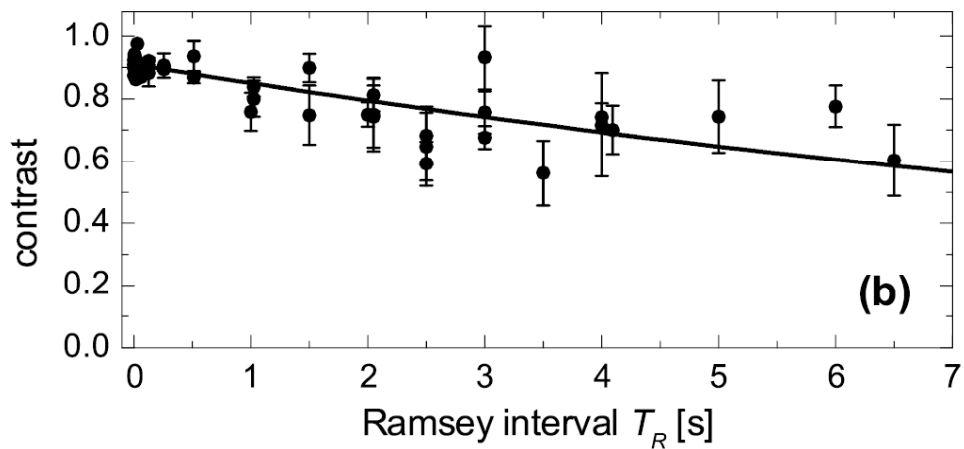


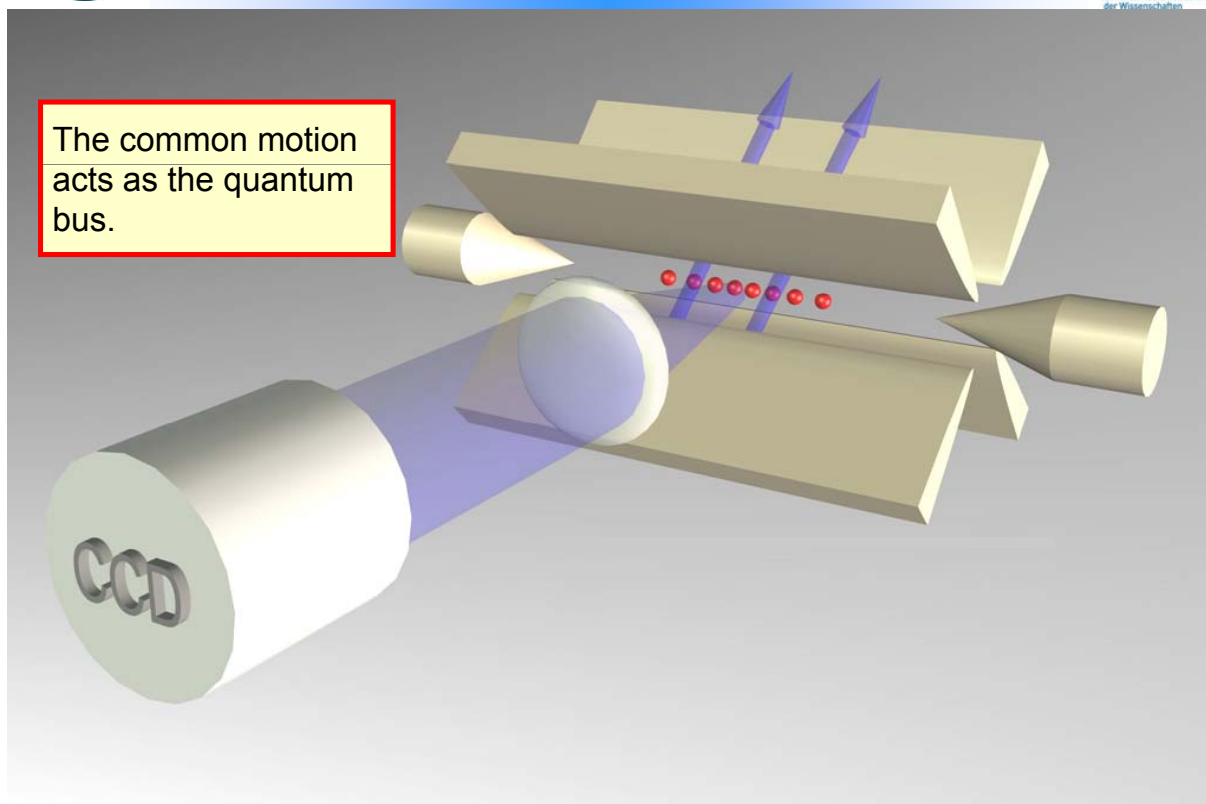
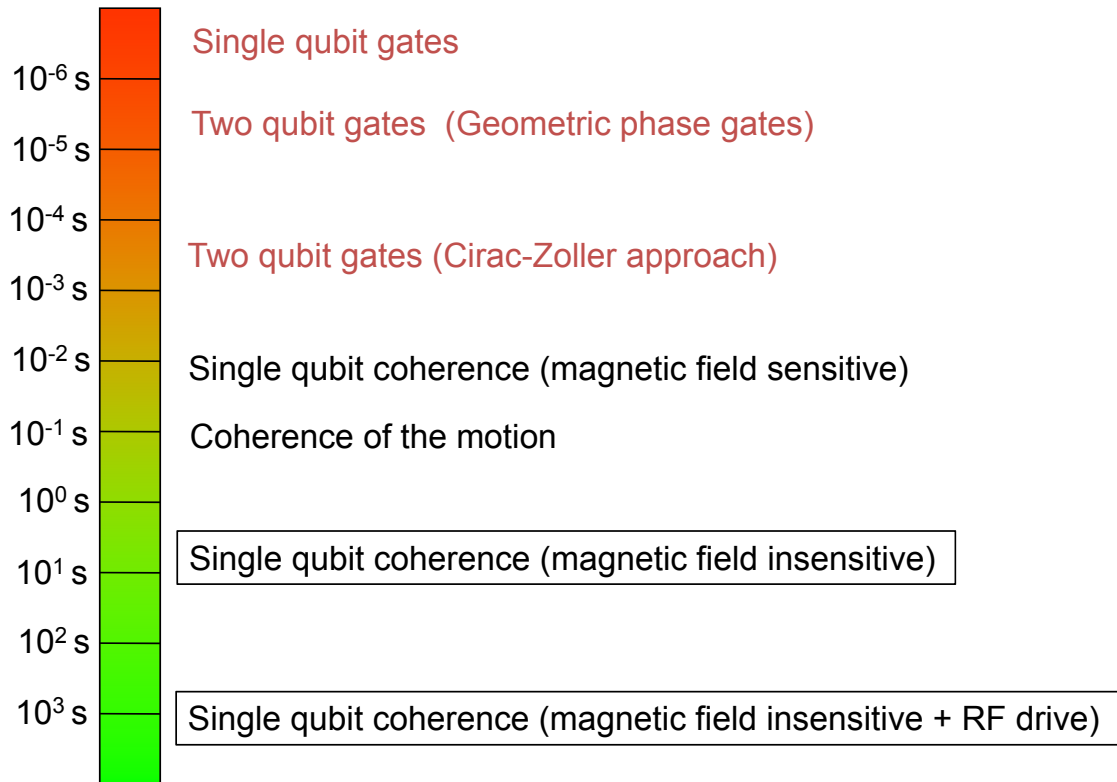
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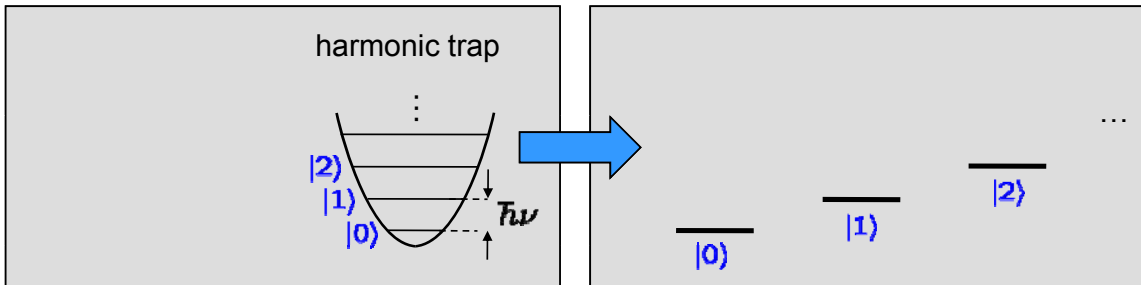
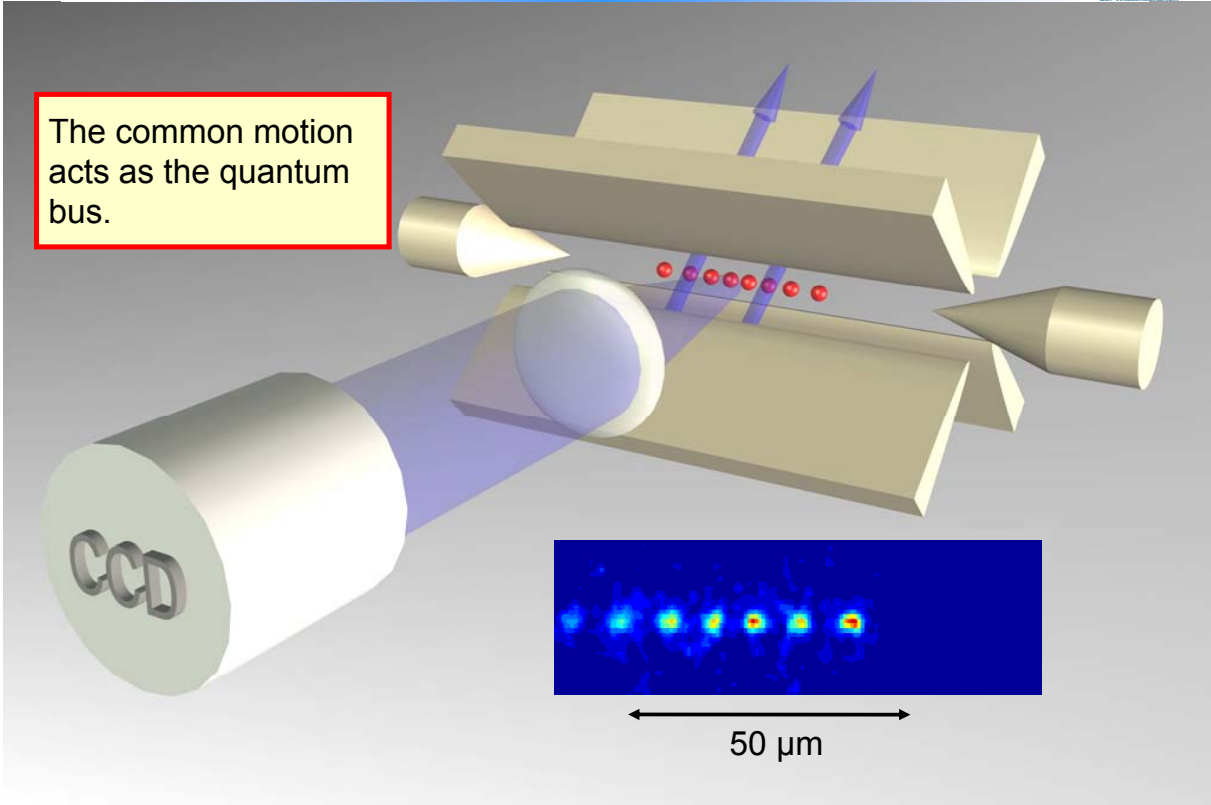
Ground state

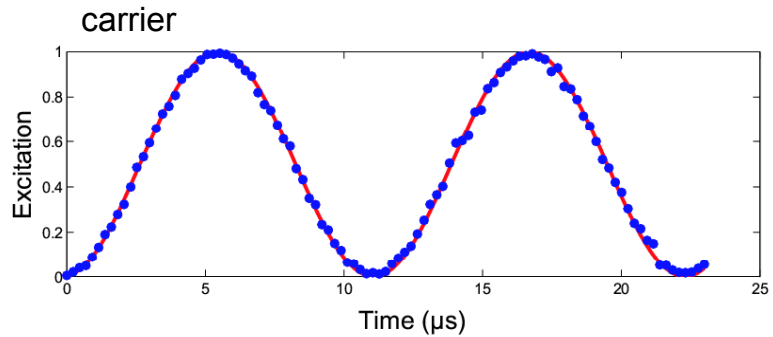
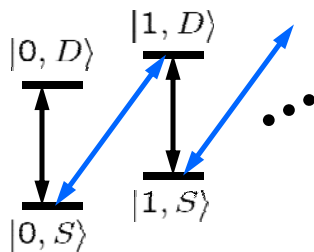
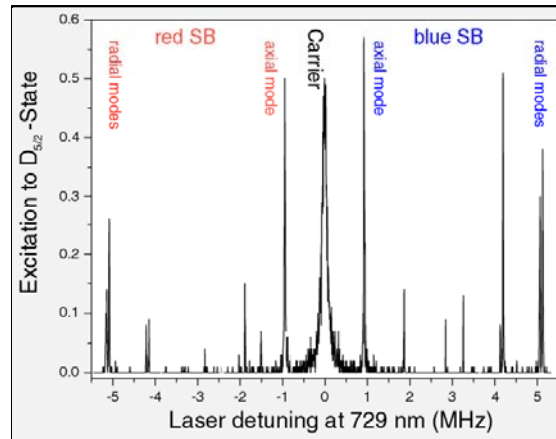
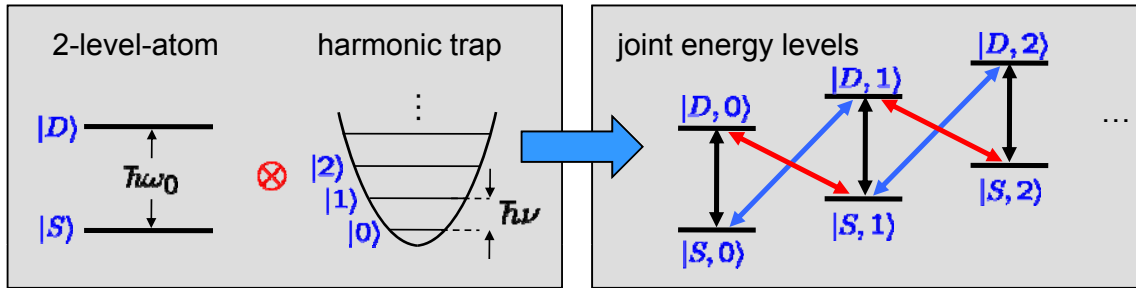


Level scheme of ${}^9\text{Be}^+$:From: C. Langer *et al.*, PRL **95**, 060502 (2005), NISTFrom: C. Langer *et al.*, PRL **95**, 060502 (2005), NIST



The common motion acts as the quantum bus.

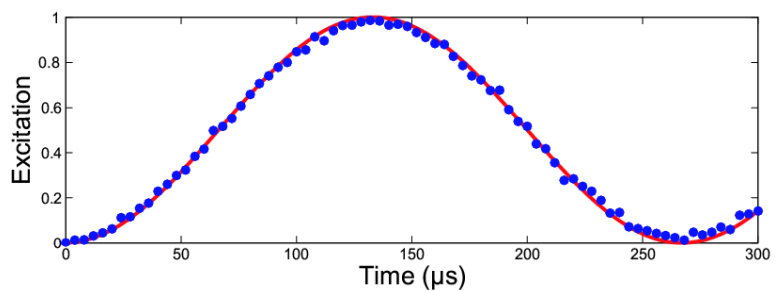




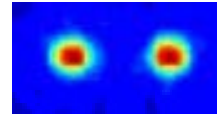
carrier and sideband Rabi oscillations with Rabi frequencies

$$\Omega, \eta\Omega$$

$\eta = kx_0$ Lamb-Dicke parameter



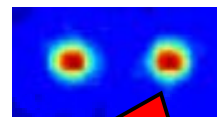
$$\begin{array}{l} \vdots \\ |DD1\rangle \text{ ---} \\ |DD0\rangle \text{ ---} \end{array}$$



$$\begin{array}{l} \vdots \\ |SD1\rangle \text{ ---} \\ |SD0\rangle \text{ ---} \end{array} \qquad \begin{array}{l} \vdots \\ \text{---} |DS1\rangle \\ \text{---} |DS0\rangle \end{array}$$

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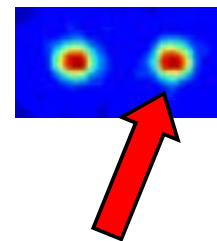
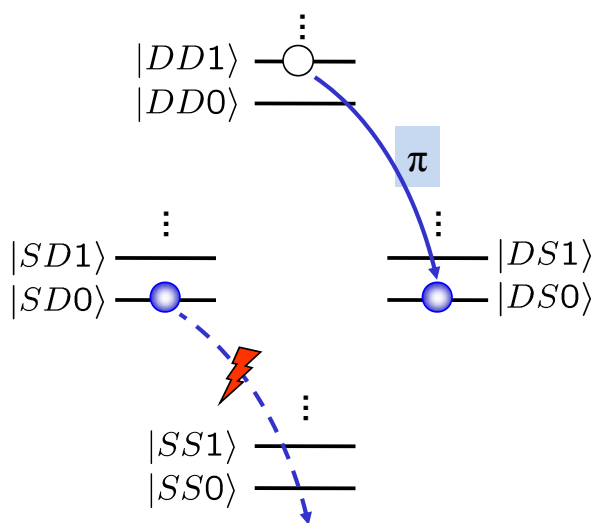
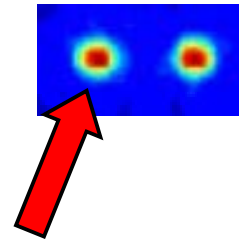
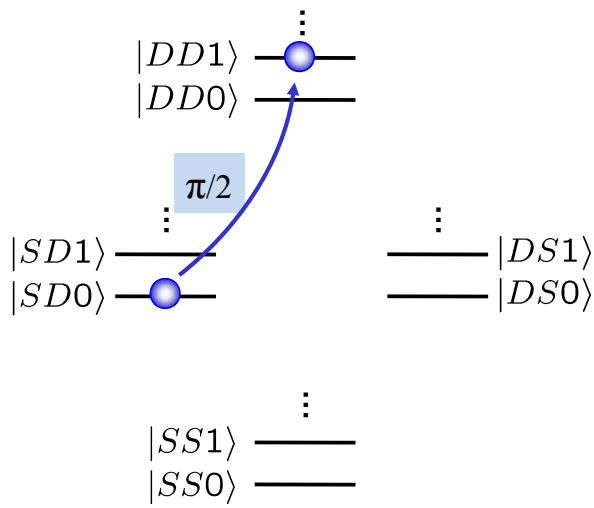
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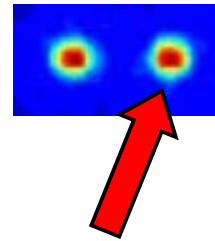
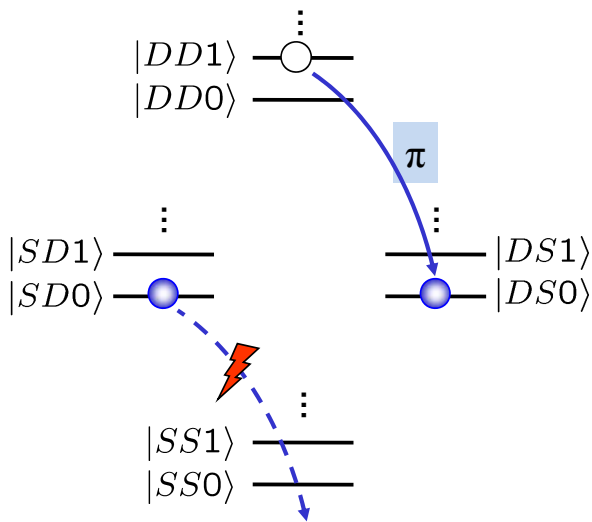


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 π

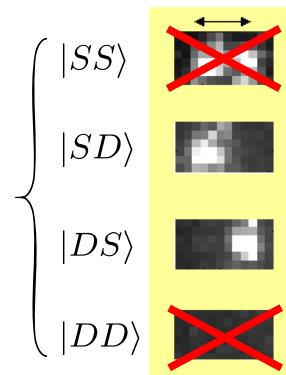


Bell states with atoms

- $^9\text{Be}^+$: NIST (fidelity: 97 %)
- $^{40}\text{Ca}^+$: Oxford (83%)
- $^{111}\text{Cd}^+$: Ann Arbor (79%)
- $^{25}\text{Mg}^+$: Munich
- $^{40}\text{Ca}^+$: Innsbruck (99%)

$$|SD\rangle + |DS\rangle$$

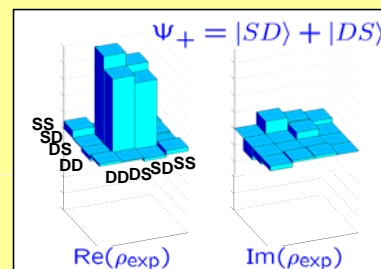
Fluorescence detection with CCD camera:



Coherent superposition or incoherent mixture ?

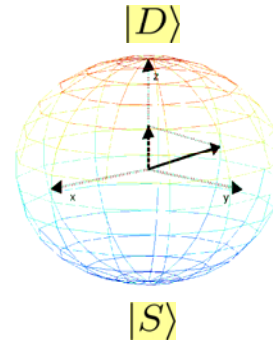
What is the relative phase of the superposition ?

➔ Measurement of the density matrix:



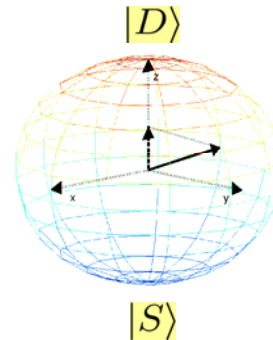
A measurement yields the z-component of the Bloch vector
 => Diagonal of the density matrix

$$\rho = \begin{pmatrix} P_S & C - iD \\ C + iD & P_D \end{pmatrix}$$

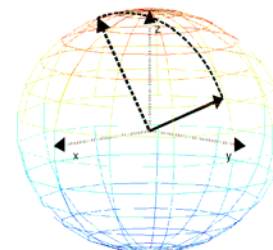


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$$\rho = \begin{pmatrix} P_S & C - iD \\ C + iD & P_D \end{pmatrix}$$



Rotation around the x- or the y-axis prior to the measurement yields the phase information of the qubit.

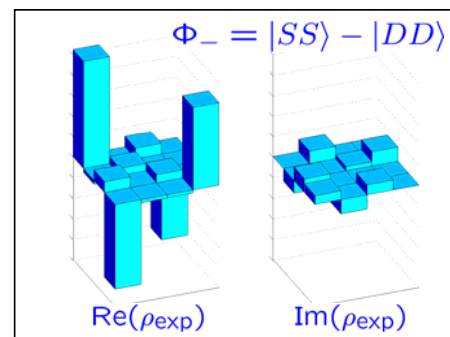
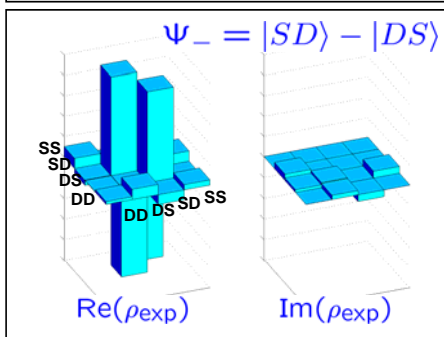
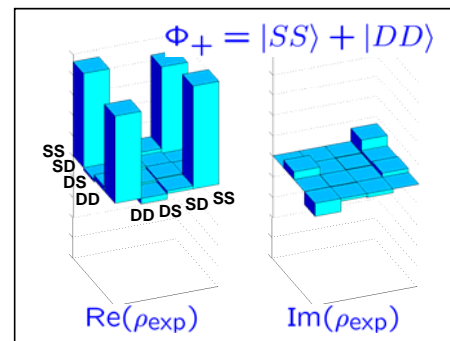
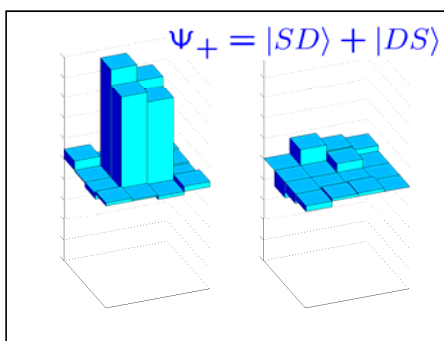
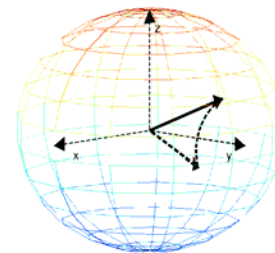
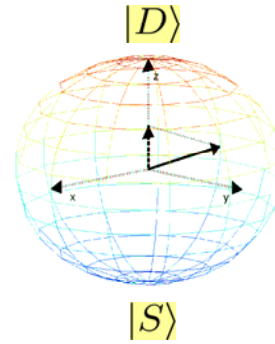


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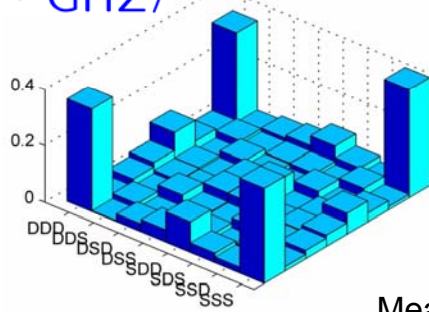
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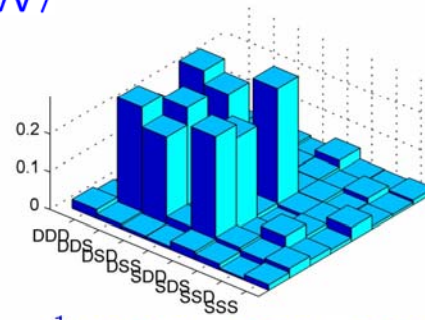
=> coherences of the density matrix



$$|\Psi_{GHZ}\rangle$$

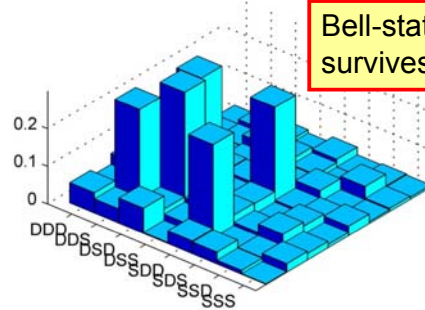
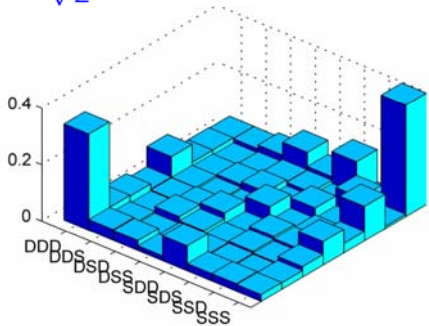


$$|\Psi_W\rangle$$



$$\frac{1}{\sqrt{2}}(|SSS\rangle + |DDD\rangle)$$

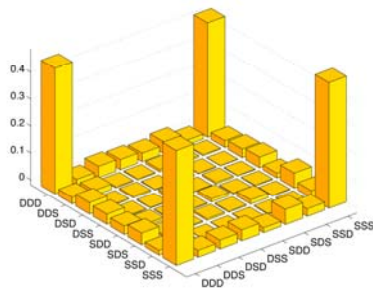
Measurement of the center ion $\frac{1}{\sqrt{3}}(|SDD\rangle + |DSD\rangle + |DDS\rangle)$



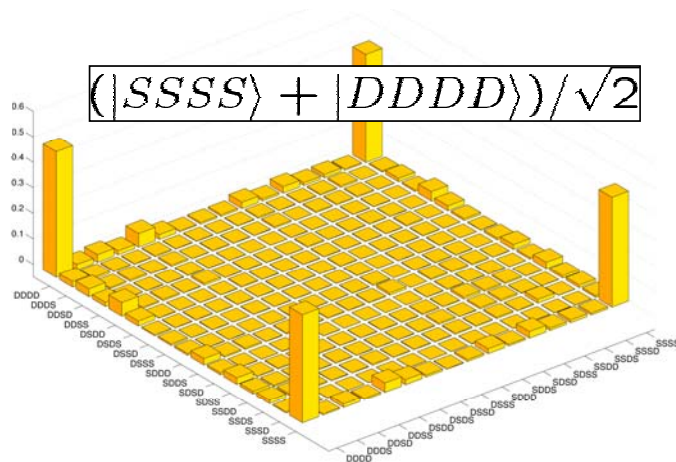
Bell-state survives

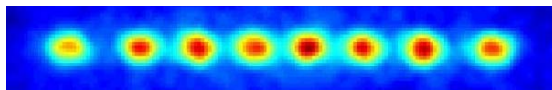
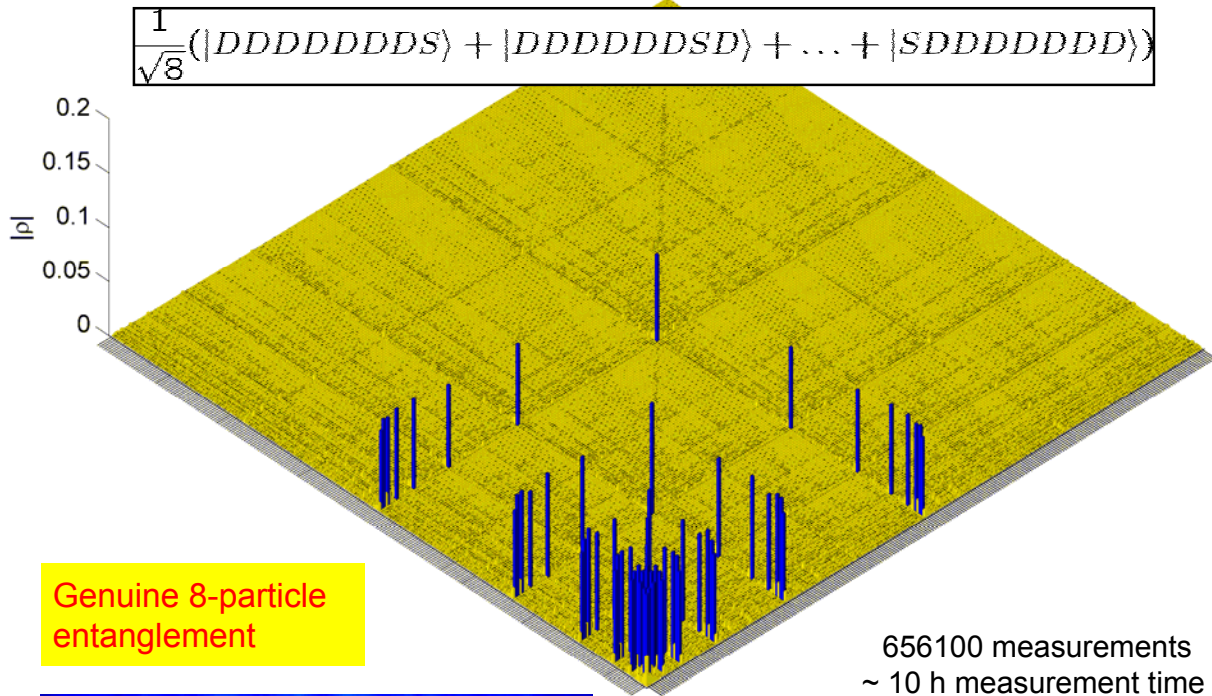
Roos et al., *Science* **304**, 1478 (2003)

$$(|SSS\rangle + |DDD\rangle)/\sqrt{2}$$



$$(|SSSS\rangle + |DDDD\rangle)/\sqrt{2}$$





Häffner et al., Nature **438**, 643 (2005)

- I. Scalable physical system, well characterized qubits
- II. Ability to initialize the state of the qubits
- III. Long relevant coherence times, much longer than gate operation time
- IV. “Universal” set of quantum gates
- V. Qubit-specific measurement capability

Quantum gates ...



Having the qubits interact



VOLUME 74, NUMBER 20 PHYSICAL REVIEW LETTERS 15 MAY 1995

Quantum Computations with Cold Trapped Ions

J. I. Cirac and P. Zoller*

*Institut für Theoretische Physik, Universität Innsbruck, Technikerstrasse 25, A-6020 Innsbruck, Austria
(Received 30 November 1994)*

A quantum computer can be implemented with cold ions confined in a linear trap and interacting with laser beams. Quantum gates involving any pair, triplet, or subset of ions can be realized by coupling the ions through the collective quantized motion. In this system decoherence is negligible, and the measurement (readout of the quantum register) can be carried out with a high efficiency.

PACS numbers: 89.80.+h, 03.65.Bz, 12.20.Fv, 32.80.Pj

...allows the realization of a
universal quantum computer !

$$|D\rangle|D\rangle \rightarrow |D\rangle|D\rangle$$

$$|D\rangle|S\rangle \rightarrow |D\rangle|S\rangle$$

$$|S\rangle|D\rangle \rightarrow |D\rangle|S\rangle$$

$$|S\rangle|S\rangle \rightarrow |S\rangle|D\rangle$$

control target

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$$|S\rangle|S\rangle \rightarrow |S\rangle|D\rangle$$

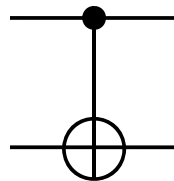
control target

Most popular gates:

- Cirac-Zoller gate (Schmidt-Kaler et al., Nature **422**, 408 (2003)).
- Geometric phase gate (Leibfried et al., Nature **422**, 412 (2003)).
- Mølmer-Sørensen gate (Sackett et al., Nature **404**, 256 (2000)).

Control bit

Target bit



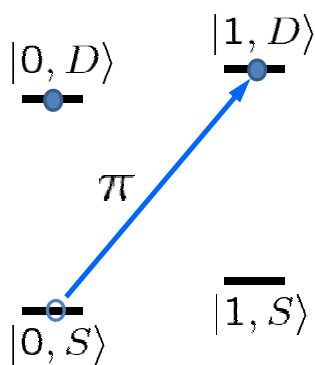
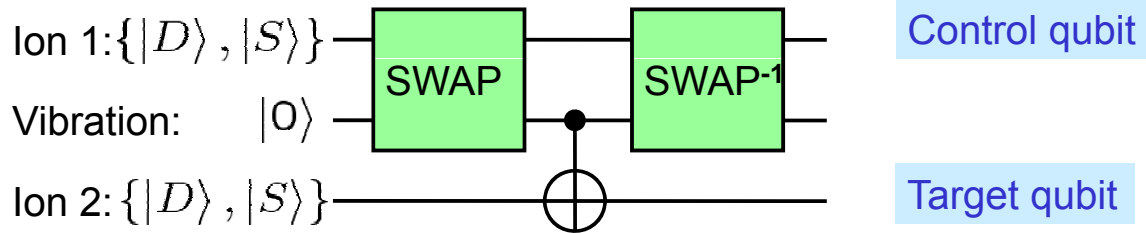
$$|0\rangle|0\rangle \rightarrow |0\rangle|0\rangle$$

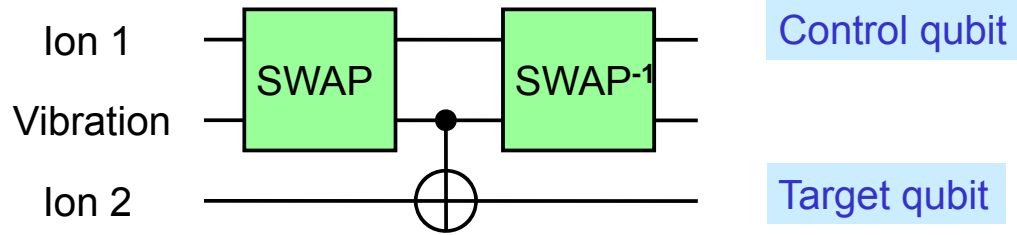
$$|0\rangle|1\rangle \rightarrow |0\rangle|1\rangle$$

$$|1\rangle|0\rangle \rightarrow |1\rangle|1\rangle$$

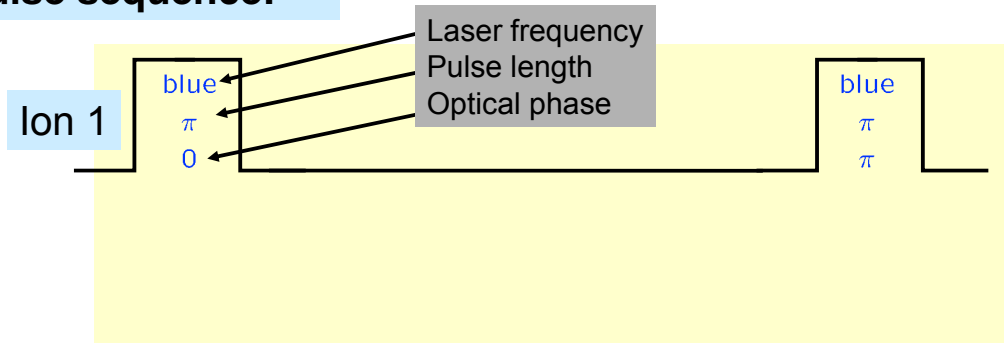
$$|1\rangle|1\rangle \rightarrow |1\rangle|0\rangle$$

Target

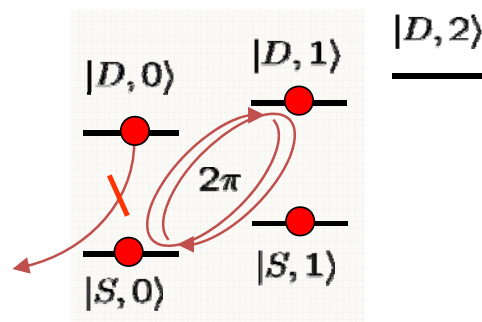




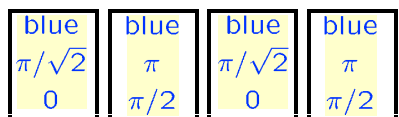
Pulse sequence:

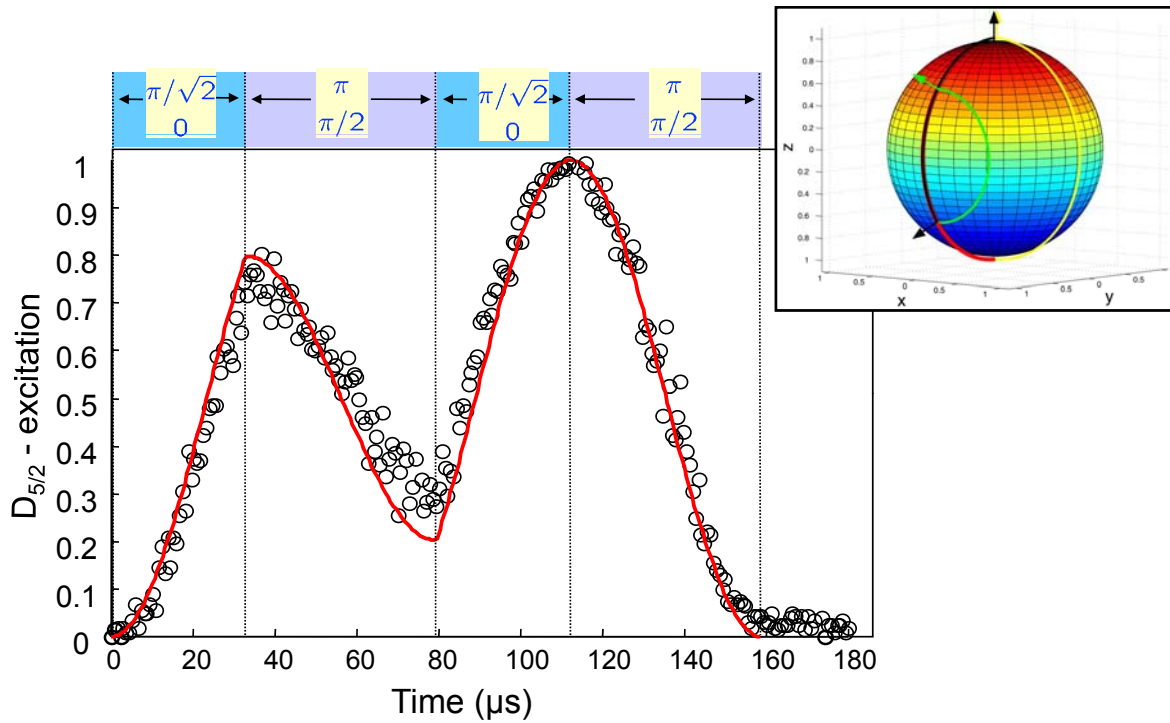
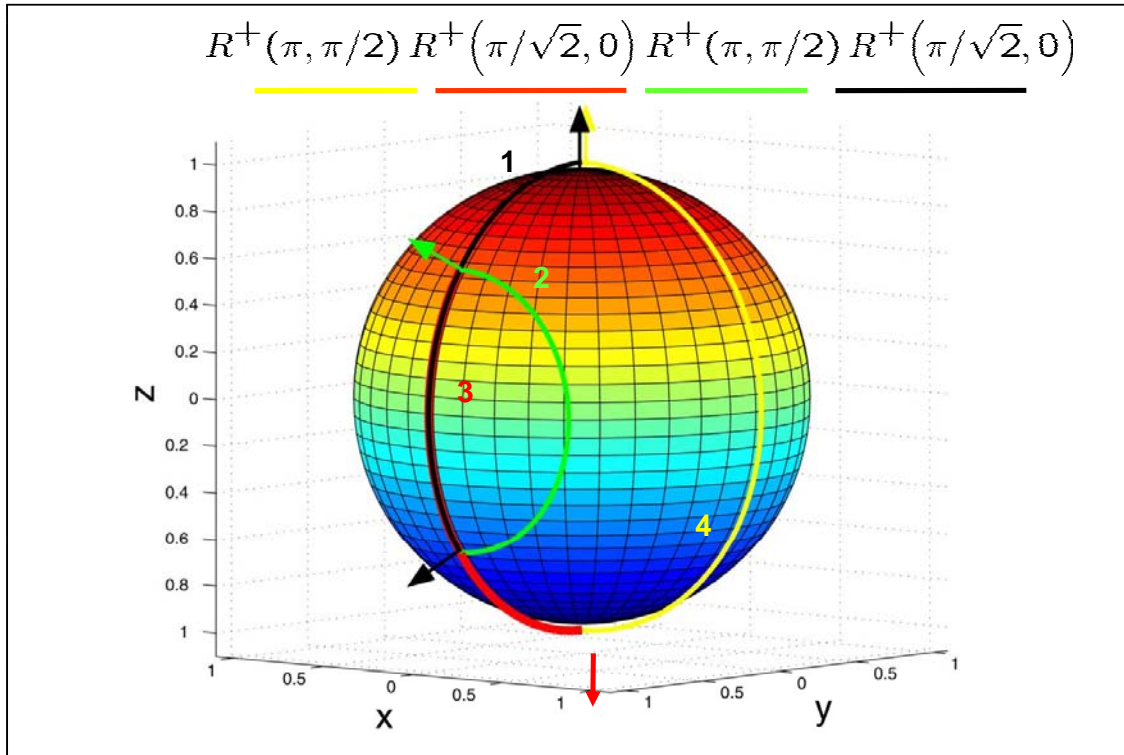


$$U_{\Phi} = \begin{matrix} & |D, 0\rangle & |S, 0\rangle & |D, 1\rangle & |S, 1\rangle \\ \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix} \end{matrix}$$

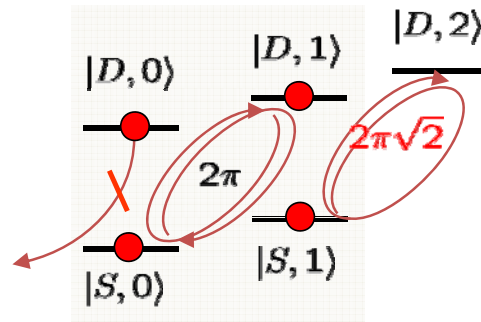


Composite 2π -rotation:





$$U_{\Phi} = \begin{matrix} & |D, 0\rangle & |S, 0\rangle & |D, 1\rangle & |S, 1\rangle \\ \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & ? \end{pmatrix} \end{matrix}$$

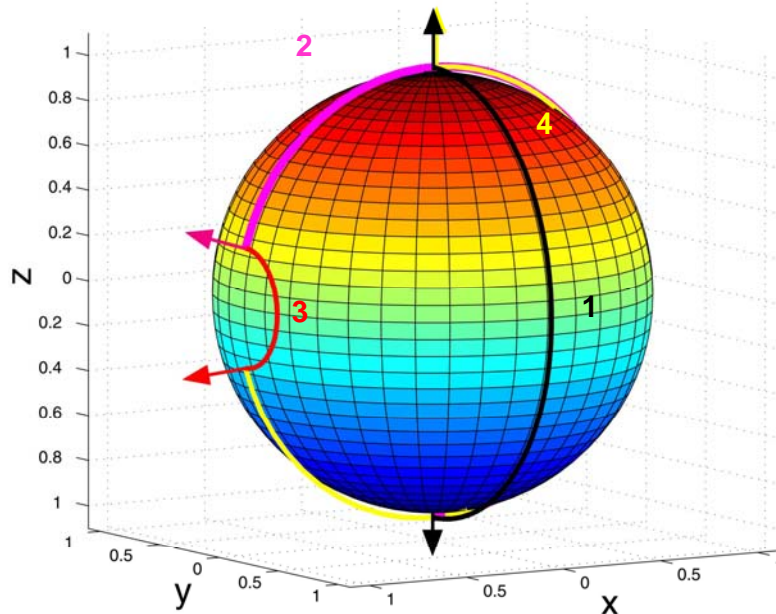


Composite 2π -rotation:

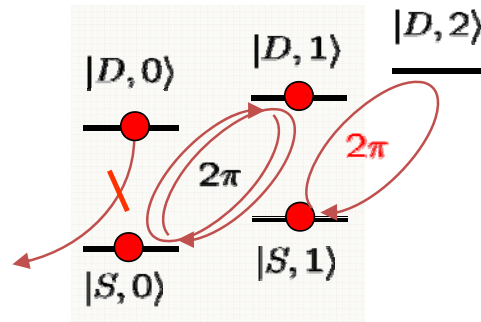
$$a^{\dagger} |n\rangle = \sqrt{n+1} |n+1\rangle$$

blue	blue	blue	blue
$\pi/\sqrt{2}$	π	$\pi/\sqrt{2}$	π
0	$\pi/2$	0	$\pi/2$

$$R^+(\pi, \pi/2) R^+(\pi/\sqrt{2}, 0) R^+(\pi, \pi/2) R^+(\pi/\sqrt{2}, 0)$$

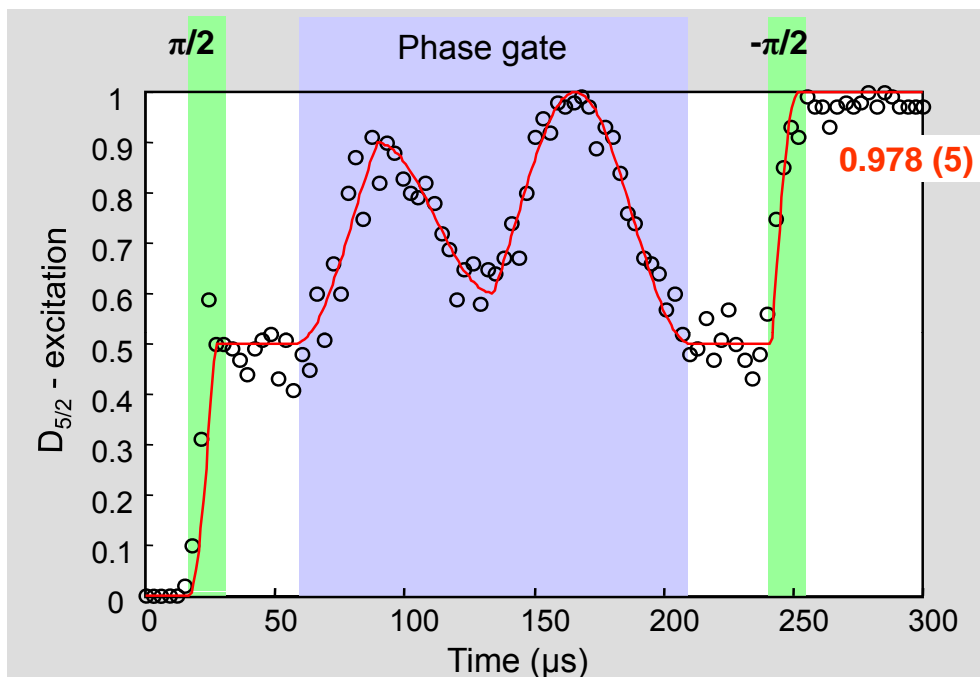


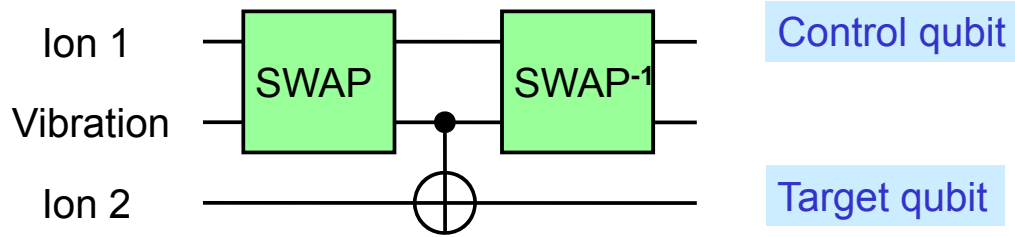
$$U_{\Phi} = \begin{pmatrix} |D,0\rangle & |S,0\rangle & |D,1\rangle & |S,1\rangle \\ 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}$$



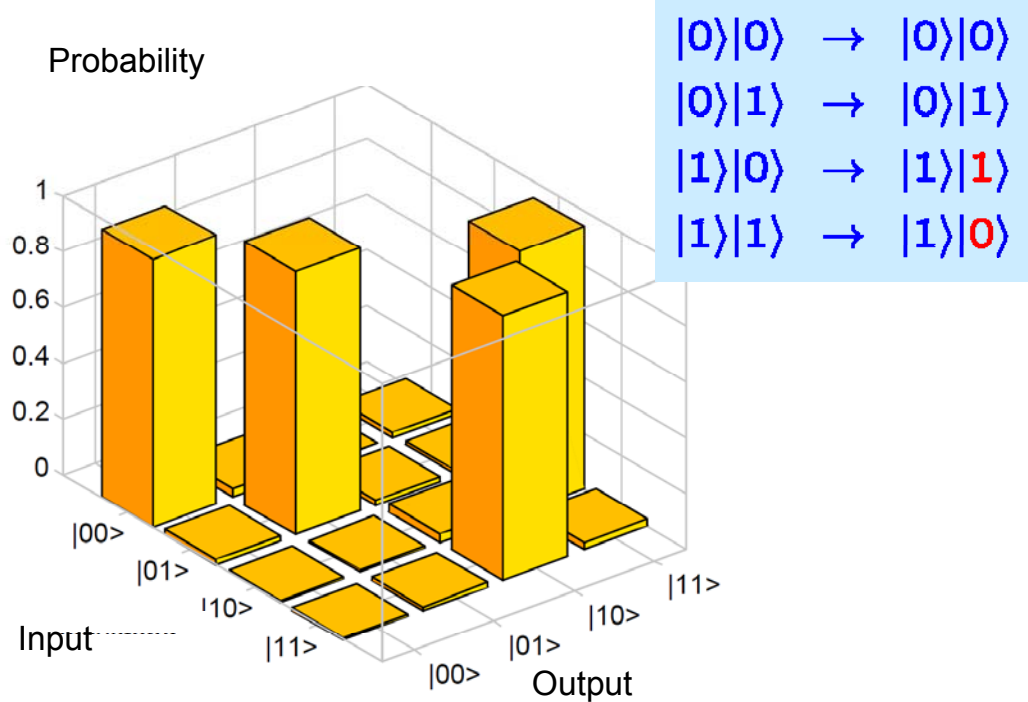
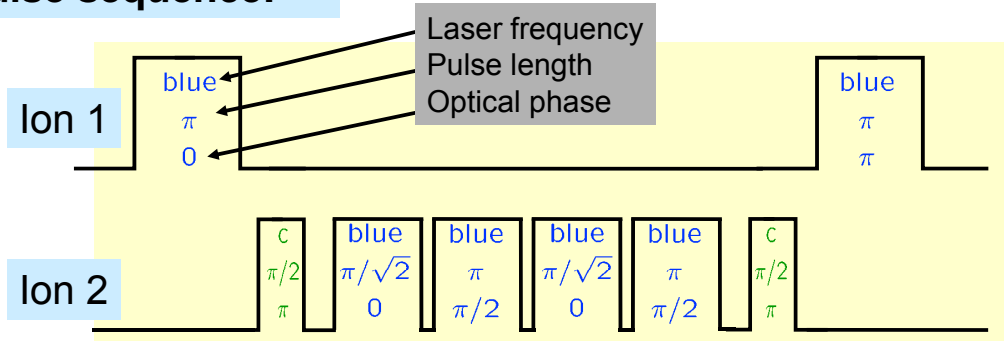
Composite 2π -rotation:

blue	blue	blue	blue
$\pi/\sqrt{2}$	π	$\pi/\sqrt{2}$	π
0	$\pi/2$	0	$\pi/2$

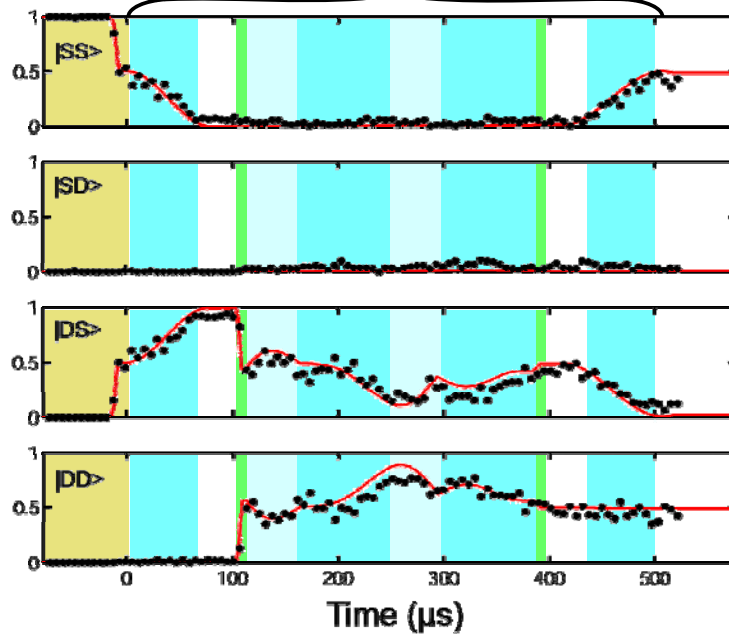




Pulse sequence:



$$|SS\rangle \xrightarrow{\text{prepare}} |S+D\rangle|S\rangle \xrightarrow{\text{CNOT}} |SS\rangle + |DD\rangle$$

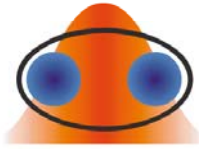


output



Draw backs of the Cirac-Zoller gate:

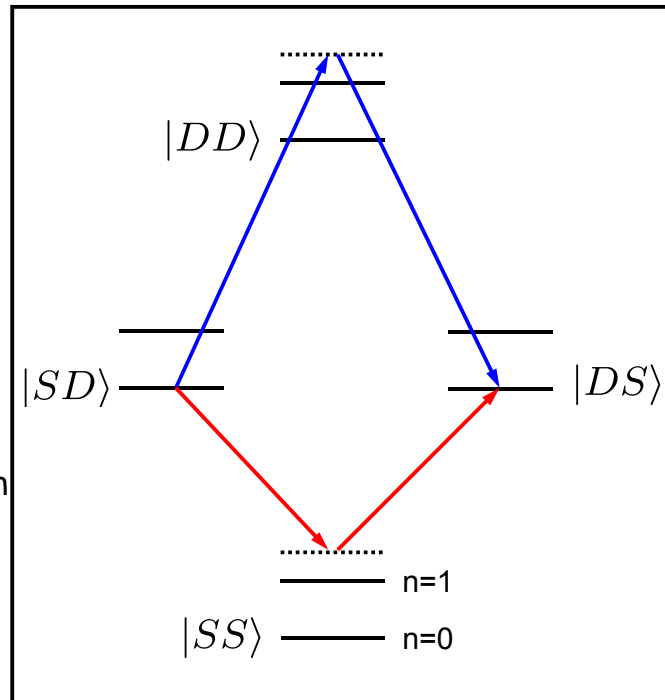
- slow (200 trap periods)
- single ion addressing required



Raman transitions between

$$|SD\rangle \Leftrightarrow |DS\rangle$$

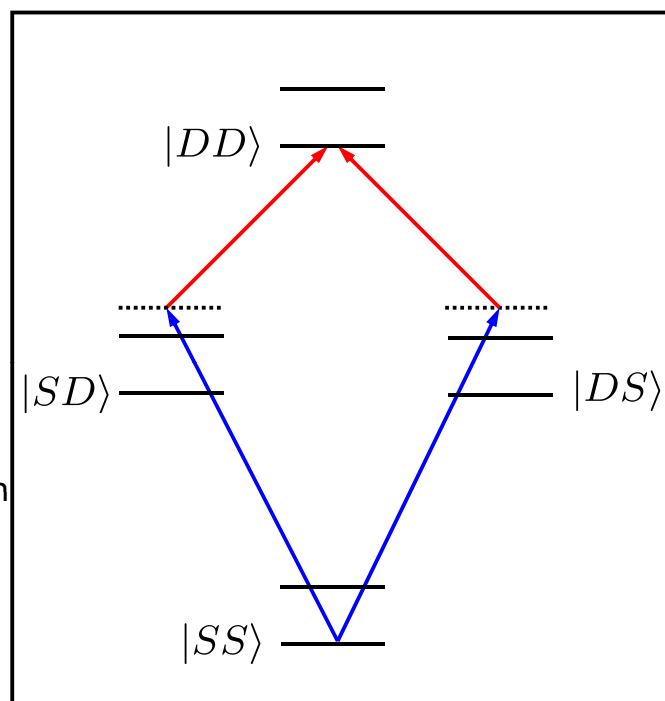
Interaction of two ions via common motion.



Raman transitions between

$$|SS\rangle \Leftrightarrow |DD\rangle$$

Interaction of two ions via common motion.

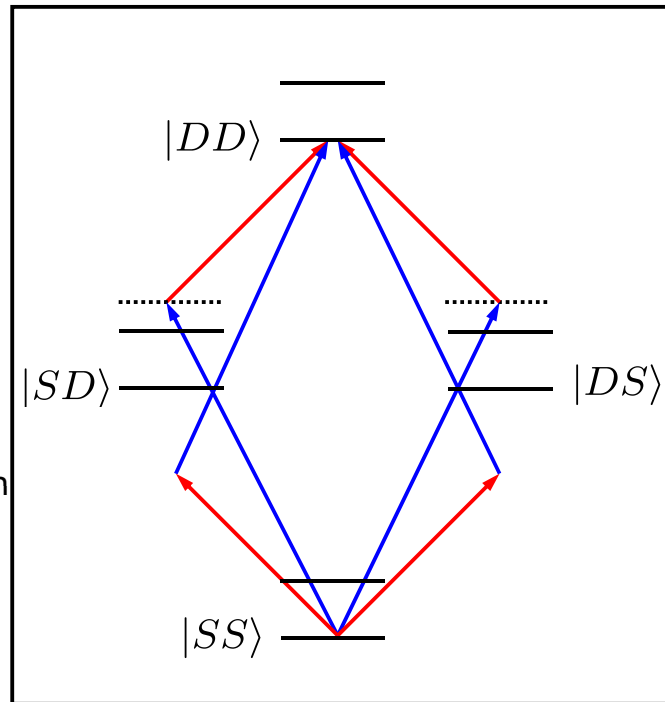




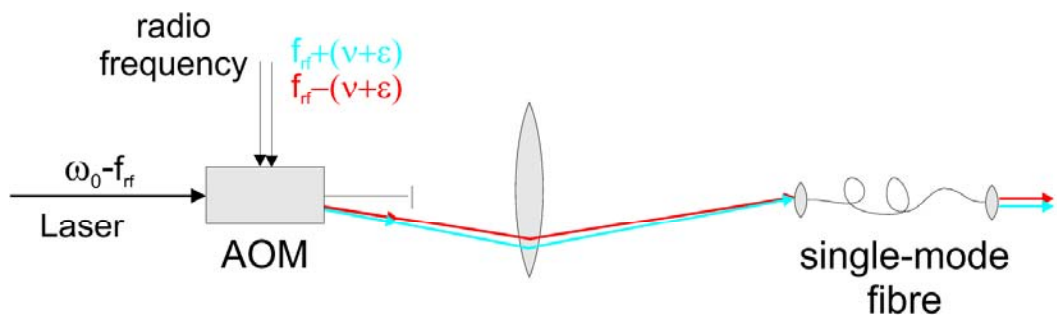
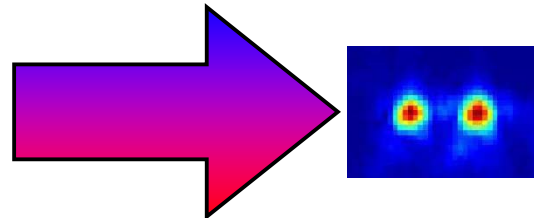
Raman transitions between

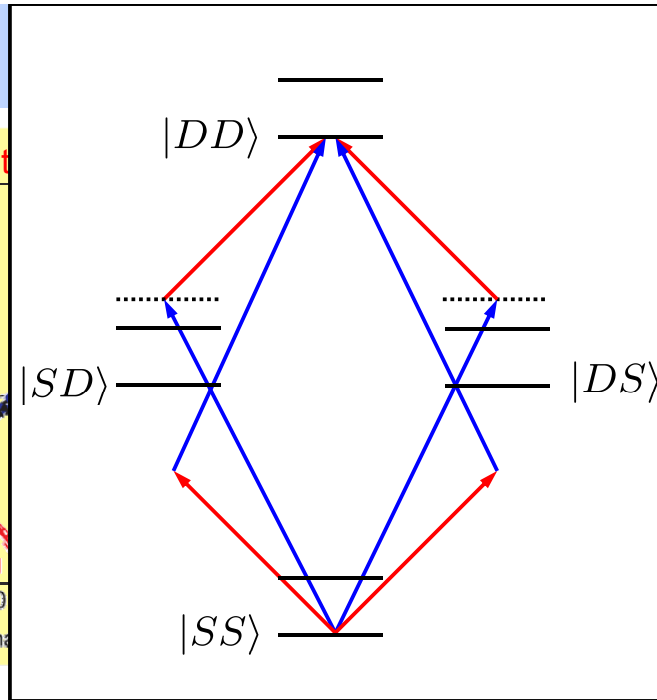
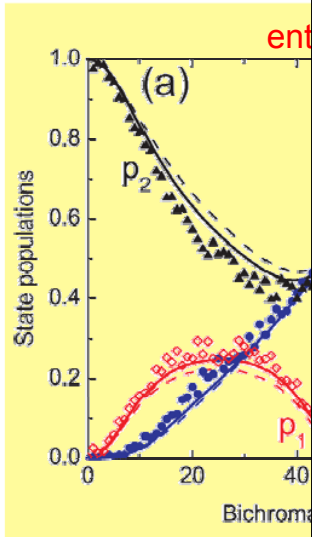
$$|SS\rangle \Leftrightarrow |DD\rangle$$

Interaction of two ions via common motion.



bichromatic beam
applied to both ions

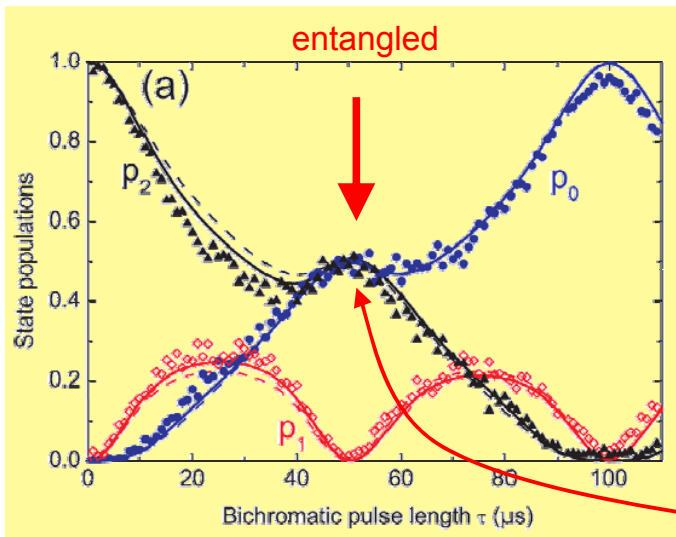




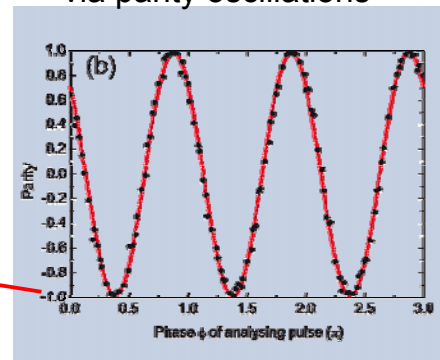
J. Benhelm et al., Nature Physics 4, 463 (2008)

Theory: C. Roos, NJP 10, 013002 (2008)

Entangling ions



measure entanglement
via parity oscillations



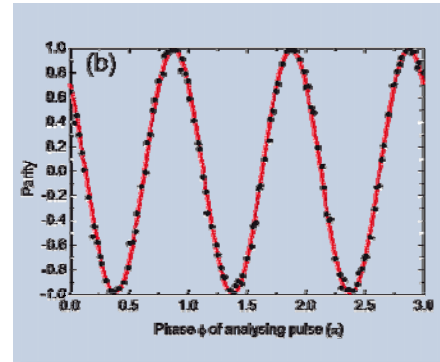
gate duration $51\mu\text{s}$

average fidelity: 99.3 (2) %

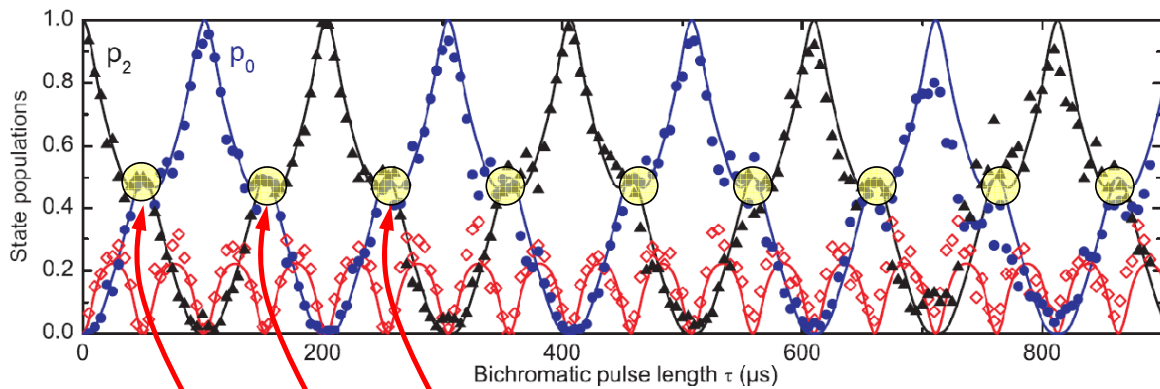
J. Benhelm et al., Nature Physics 4, 463 (2008)

Theory: C. Roos, NJP 10, 013002 (2008)

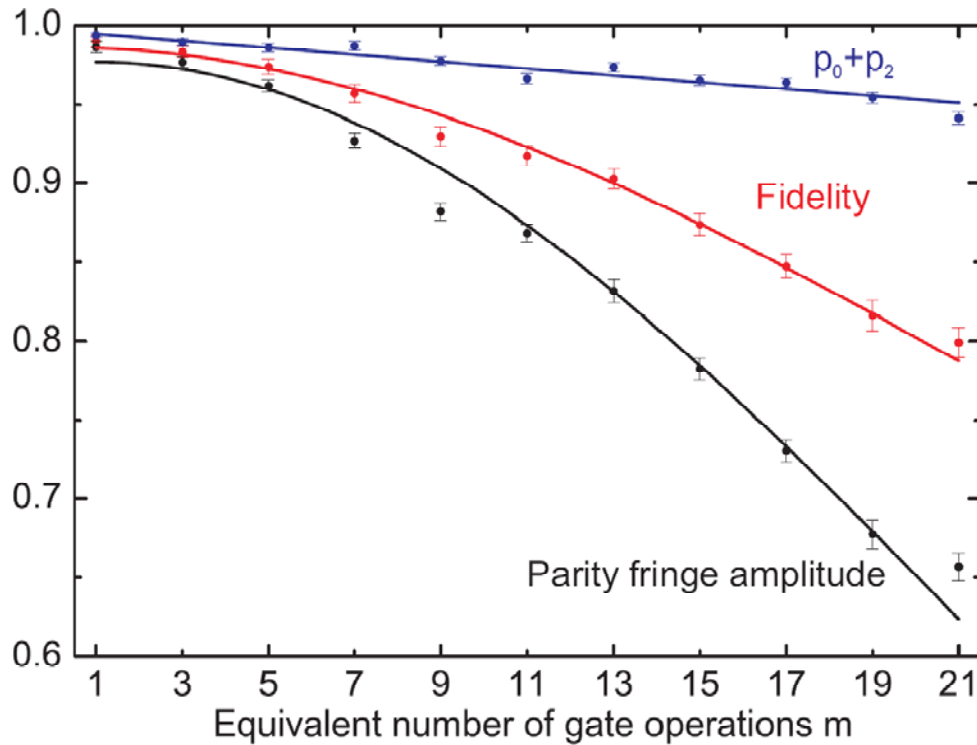
$$\begin{aligned}
 &|00\rangle + |11\rangle \xrightarrow{R_2^C(\pi/2, \varphi), R_1^C(\pi/2, \varphi)} \\
 &(|0\rangle + ie^{i\varphi}|1\rangle)(|0\rangle + ie^{i\varphi}|1\rangle) + (|1\rangle + ie^{-i\varphi}|0\rangle)(|1\rangle + ie^{-i\varphi}|0\rangle) \\
 &= (1 - e^{-2i\varphi})|00\rangle + ie^{i\varphi}(1 + e^{-2i\varphi})|01\rangle \\
 &\quad + ie^{i\varphi}(1 + e^{-2i\varphi})|10\rangle + (1 - e^{-2i\varphi})|11\rangle,
 \end{aligned}$$



Gate concatenation



maximally entangled states



Scaling of this approach?

Problems :

- Coupling strength between internal and motional states of a N-ion string decreases as

$$\eta \propto \frac{1}{\sqrt{N}}$$

(momentum transfer from photon to ion string becomes more difficult)

-> Gate operation speed slows down

- More vibrational modes increase risk of spurious excitation of unwanted modes
- Distance between neighbouring ions decreases -> addressing more difficult

-> Use flexible trap potentials to split long ion string into smaller segments and perform operations on these smaller strings

- I. Scalable physical system, well characterized qubits ✓ / ?
- II. Ability to initialize the state of the qubits ✓
- III. Long relevant coherence times, much longer than gate operation time ✓
- IV. “Universal” set of quantum gates ✓
- V. Qubit-specific measurement capability ✓

Often neglected:

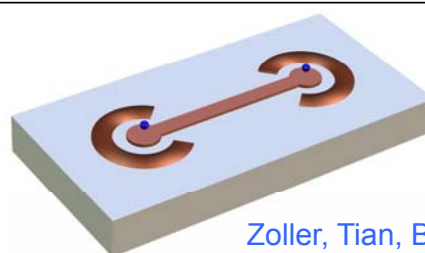
- exceptional fidelity of operations
- low error rate also for large quantum systems
- all requirements have to met at the same time

Its easy to have thousands of coherent qubits ...
but hard to control their interaction

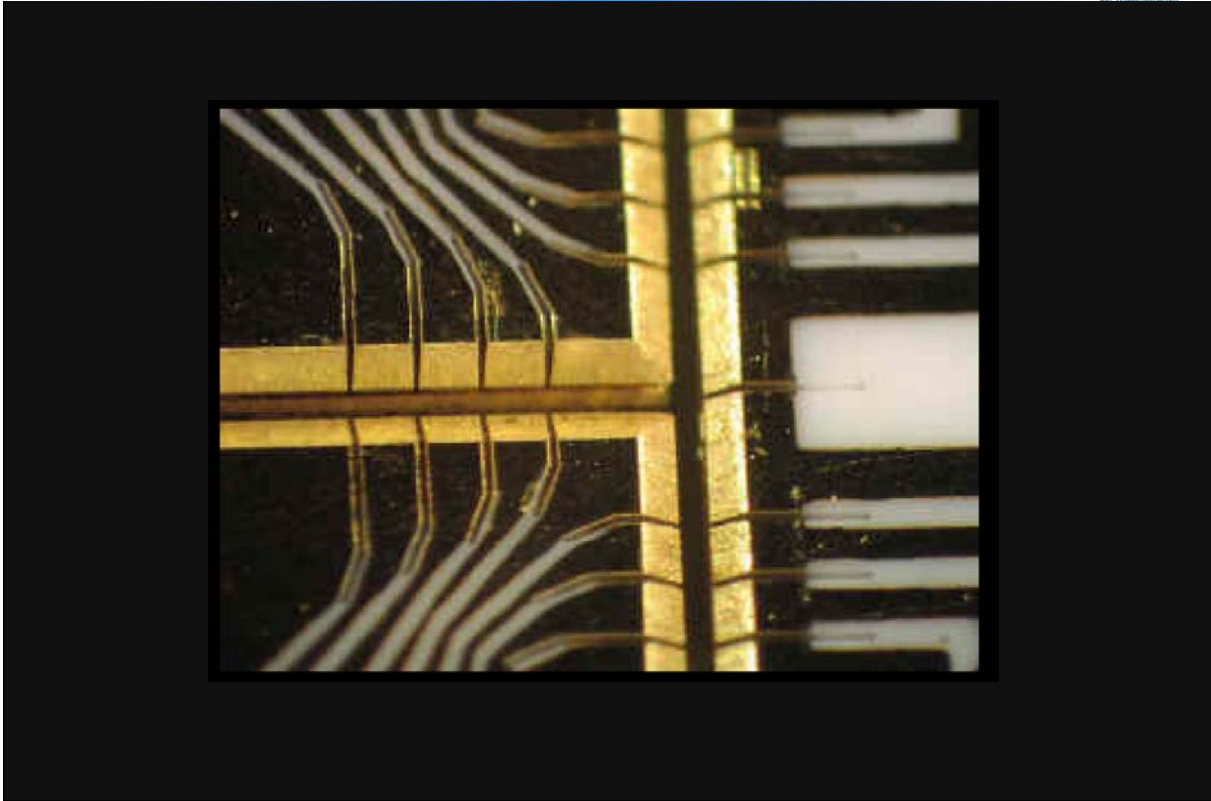
Kielpinski, Monroe, Wineland



Cirac, Zoller, Kimble, Mabuchi



Zoller, Tian, Blatt



An implementation of the Deutsch-algorithm ...

Deutsch's problem: Introduction

Decide which class the coin is:

False (equal sides)

or

Fair

Front



Back



A single measurement does **NOT** give the right answer

Deutsch's problem: Mathematical formulation

4 possible coins are represented by 4 functions

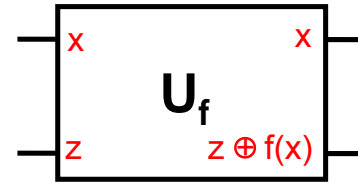
	Constant		Balanced	
	Case 1	Case 2	Case 3	Case 4
$f(0)$	0	1	0	1
$f(1)$	0	1	1	0



Deutsch's problem: Mathematical formulation

4 possible coins are represented by 4 functions

	Constant		Bal	
	Case 1	Case 2	Case 3	
$f(0)$	0	1	0	1
$f(1)$	0	1	1	0
$z \oplus f(x)$	ID	NOT	CNOT	Z-CNOT



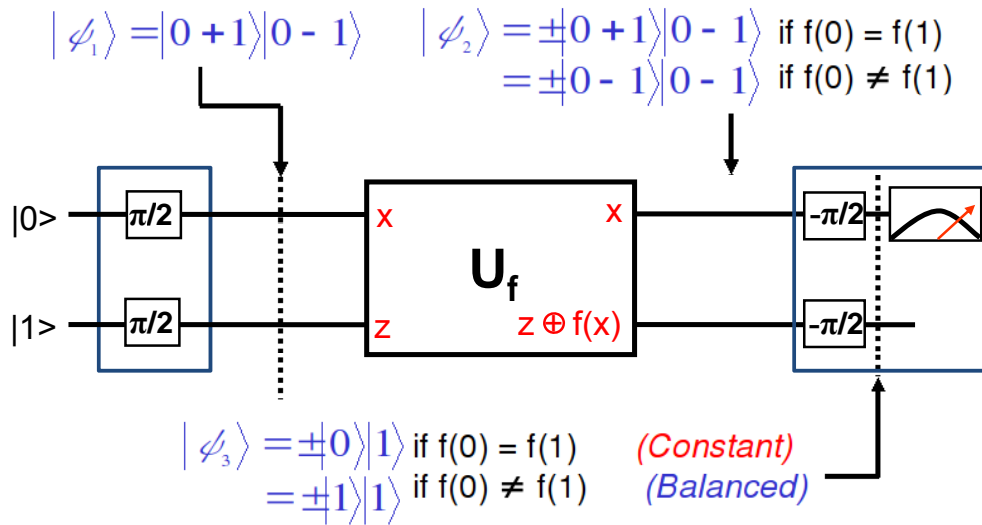
$$U_{f_n} |x, z\rangle = |x, f_n(x) \oplus z\rangle$$

Physically reversible process realized by a unitary transformation

Deutsch Jozsa quantum circuit

Case	Logic	Quantum circuit	Matrix U_{f_n}
f_1	ID		1000 0100 0010 0001
f_2	NOT		0100 1000 0001 0010
f_3	CNOT		1000 0100 0001 0010
f_4	Z-CNOT		0100 1000 0010 0001

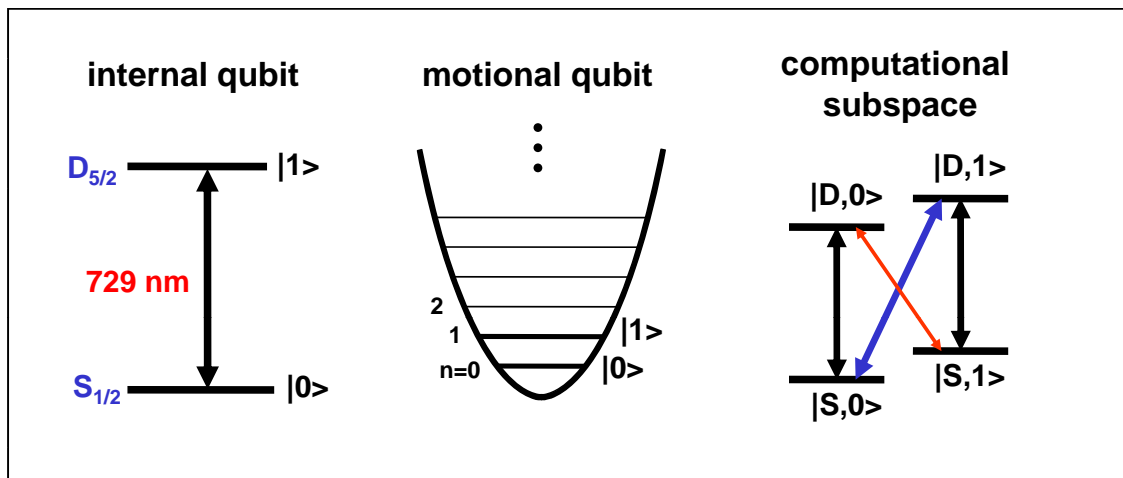
Deutsch Jozsa quantum circuit



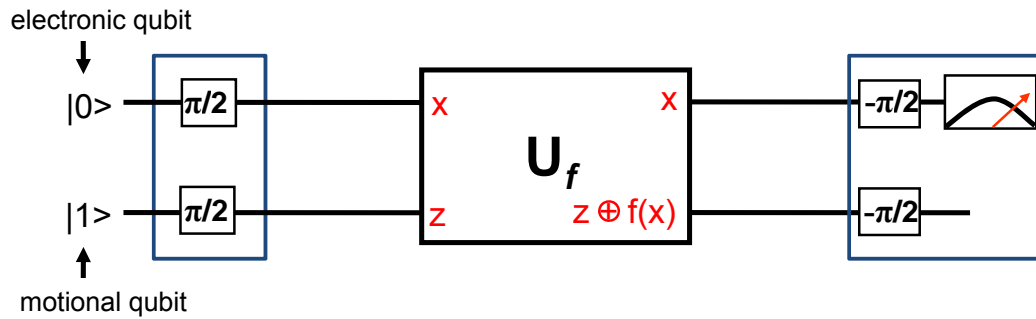
Quantum analysis gives the right answer after a **single** measurement!

- D. Deutsch, R. Jozsa, *Proc. R. Soc. London A*439, 553 (1992)
- M. Nielsen, I. Chuang, *QC and QI*, Cambridge (2000)

Qubits in $^{40}\text{Ca}^+$



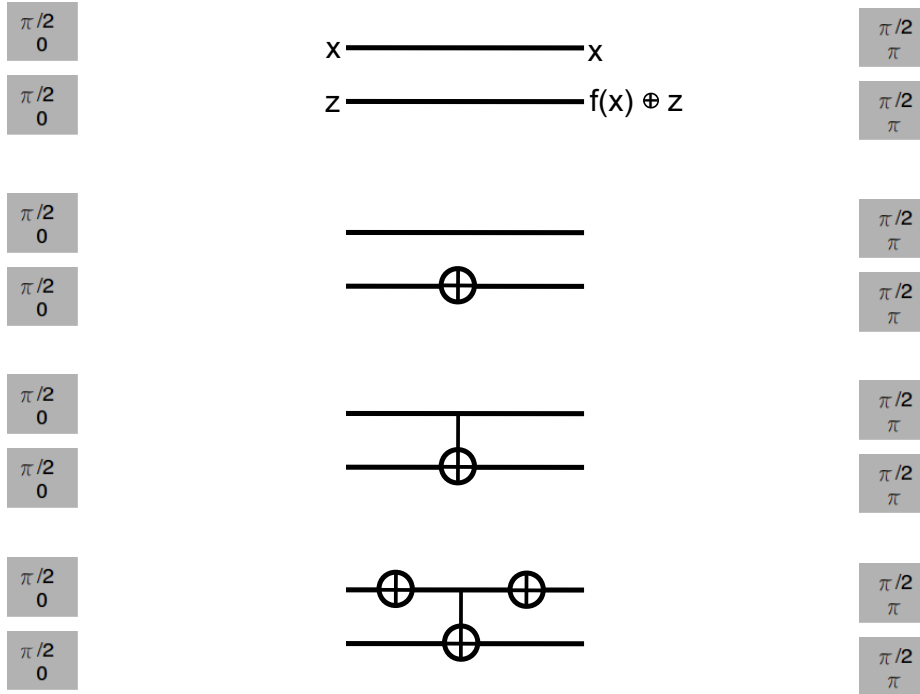
No information in the second qubit



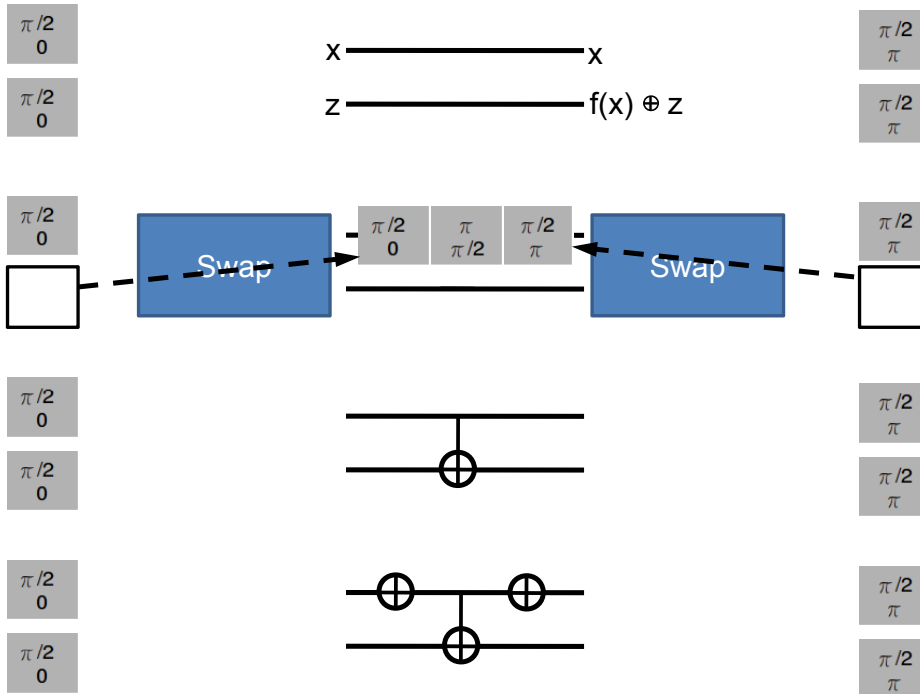
Deutsch Jozsa quantum circuit

Case	Logic	Quantum circuit	Matrix U_{in}
f_1	ID		1000 0100 0010 0001
f_2	NOT		0100 1000 0001 0010
f_3	CNOT		1000 0100 0001 0010
f_4	Z-CNOT		0100 1000 0010 0001

Deutsch Jozsa: Realization

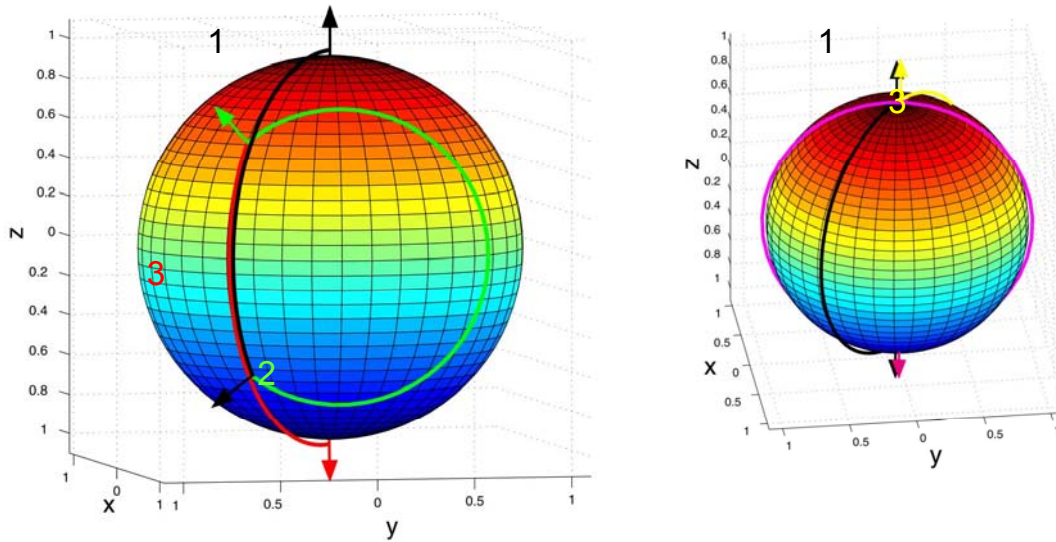


Deutsch Jozsa: Realization



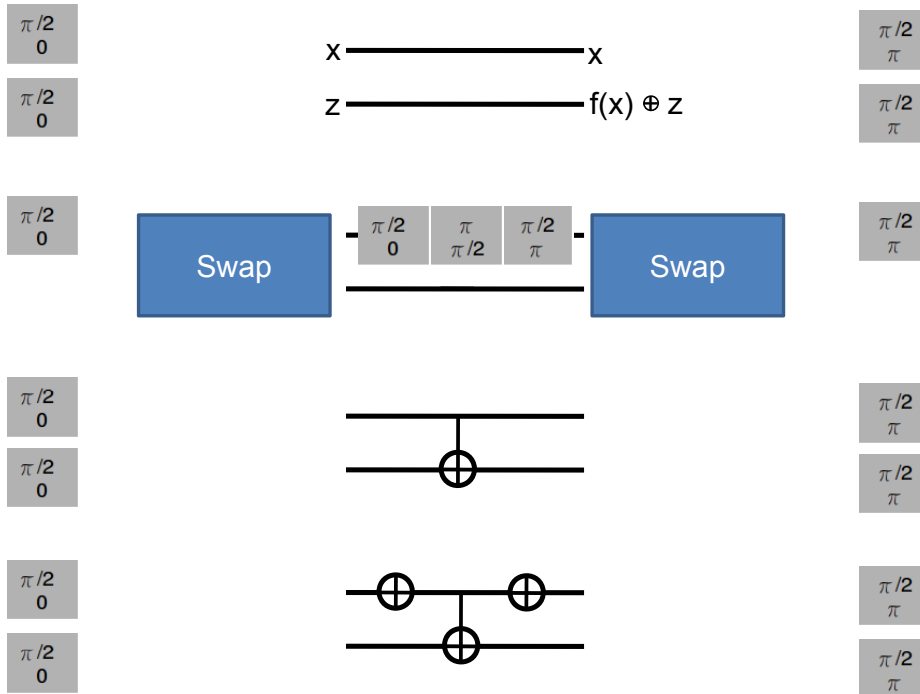
3-step composite SWAP operation

$$R^+\left(\frac{\pi}{\sqrt{2}}, \pi\right) R^+\left(\frac{2\pi}{\sqrt{2}}, \pi + \varphi_{\text{swap}}\right) R^+\left(\frac{\pi}{\sqrt{2}}, \pi\right)$$

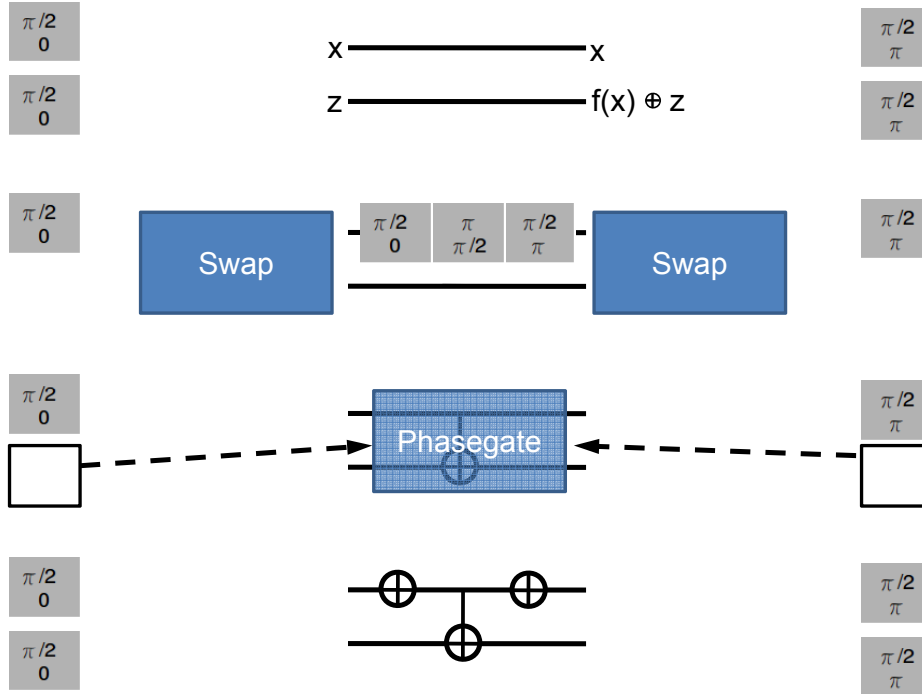


I. Chuang et al., Innsbruck (2002)

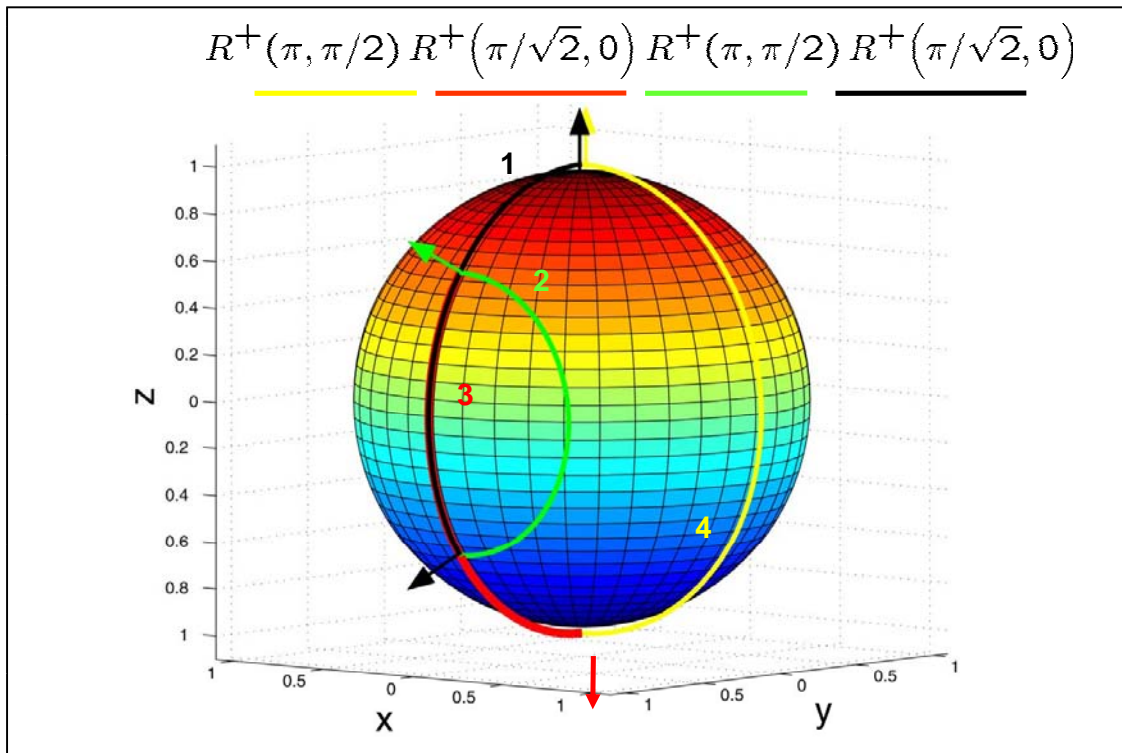
Deutsch Jozsa: Realization



Deutsch Jozsa: Realization

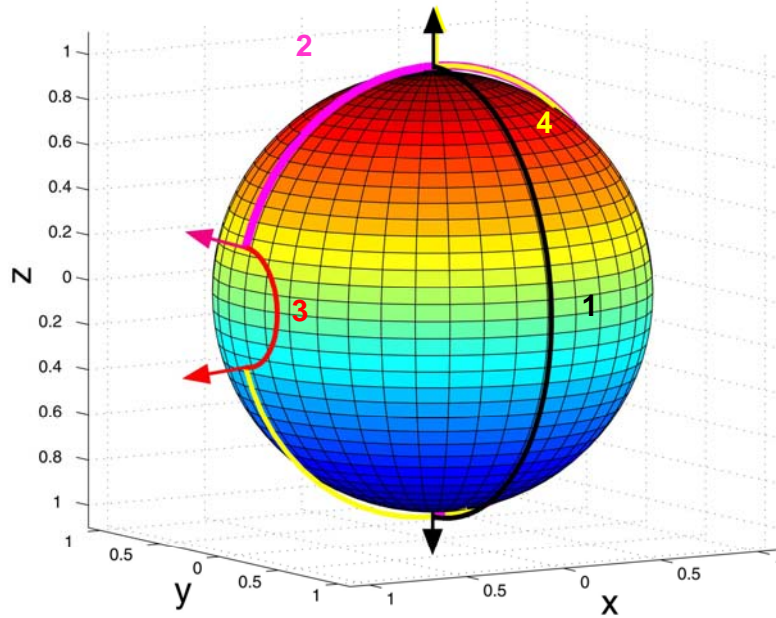


Composite phase gate (2π rotation)

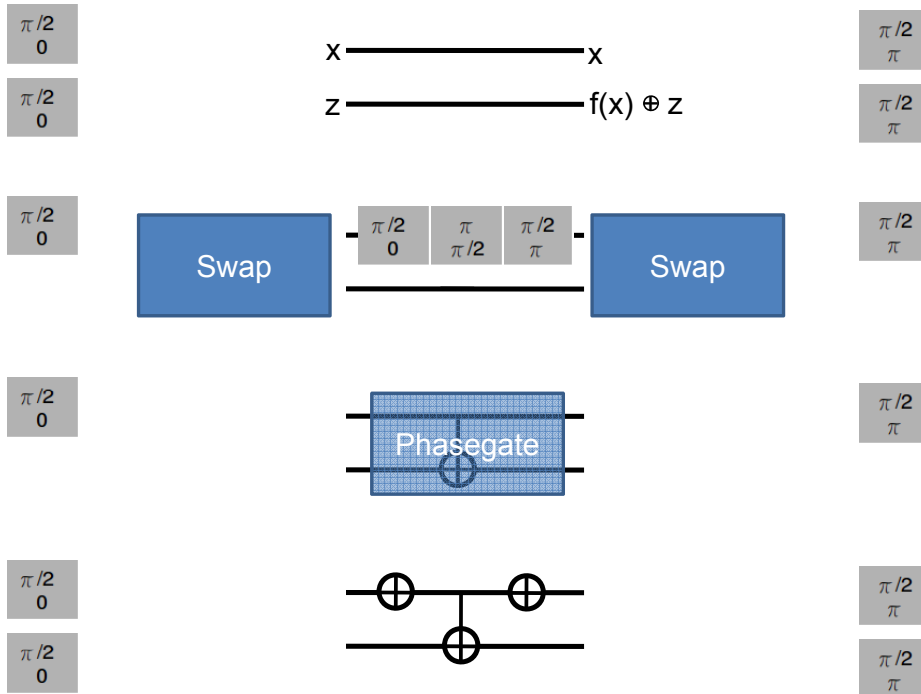


Action on $|S, 1\rangle - |D, 2\rangle$

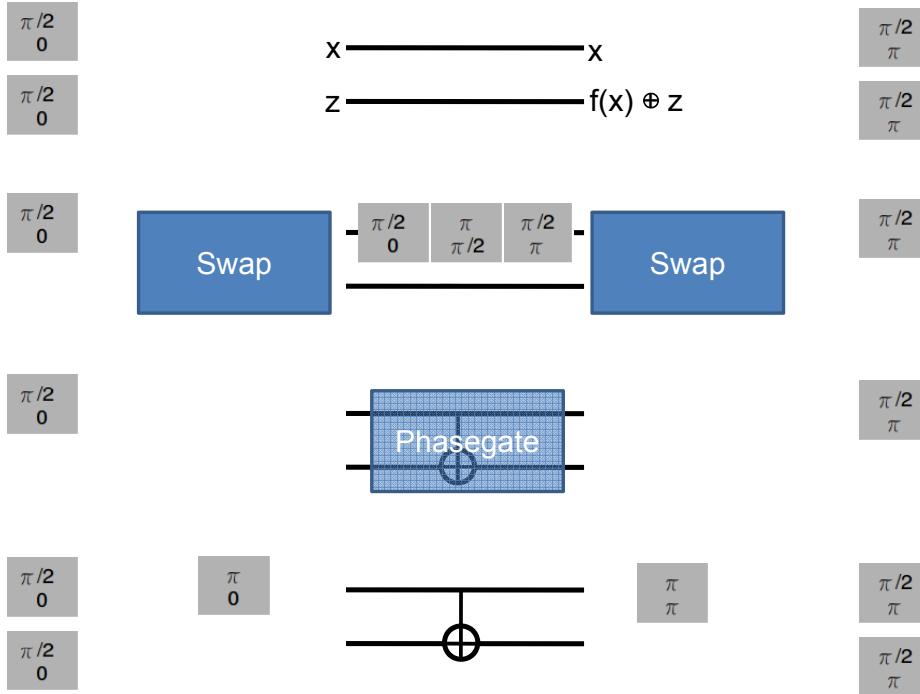
$$R^+(\pi, \pi/2) R^+(\pi/\sqrt{2}, 0) R^+(\pi, \pi/2) R^+(\pi/\sqrt{2}, 0)$$



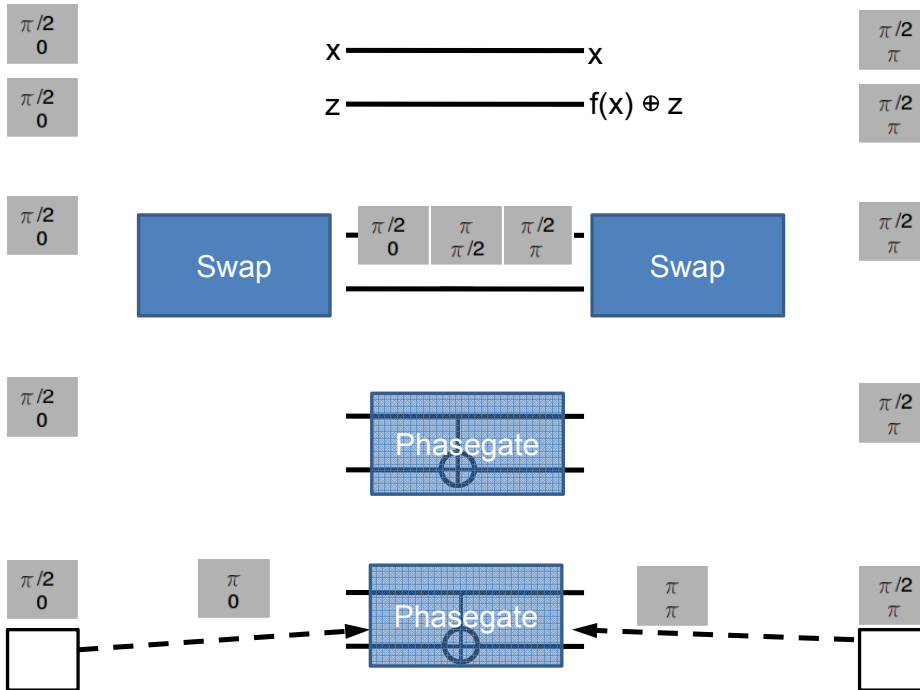
Deutsch Jozsa: Realization



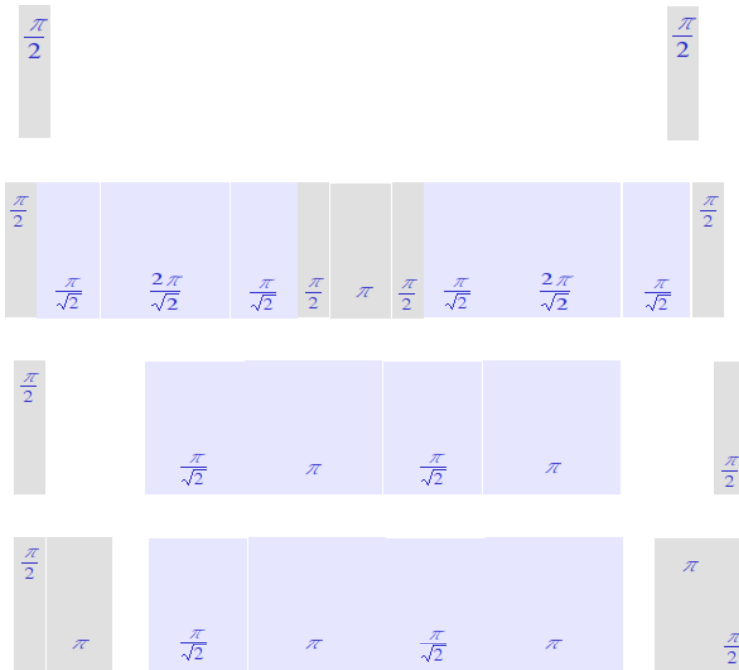
Deutsch Jozsa: Realization



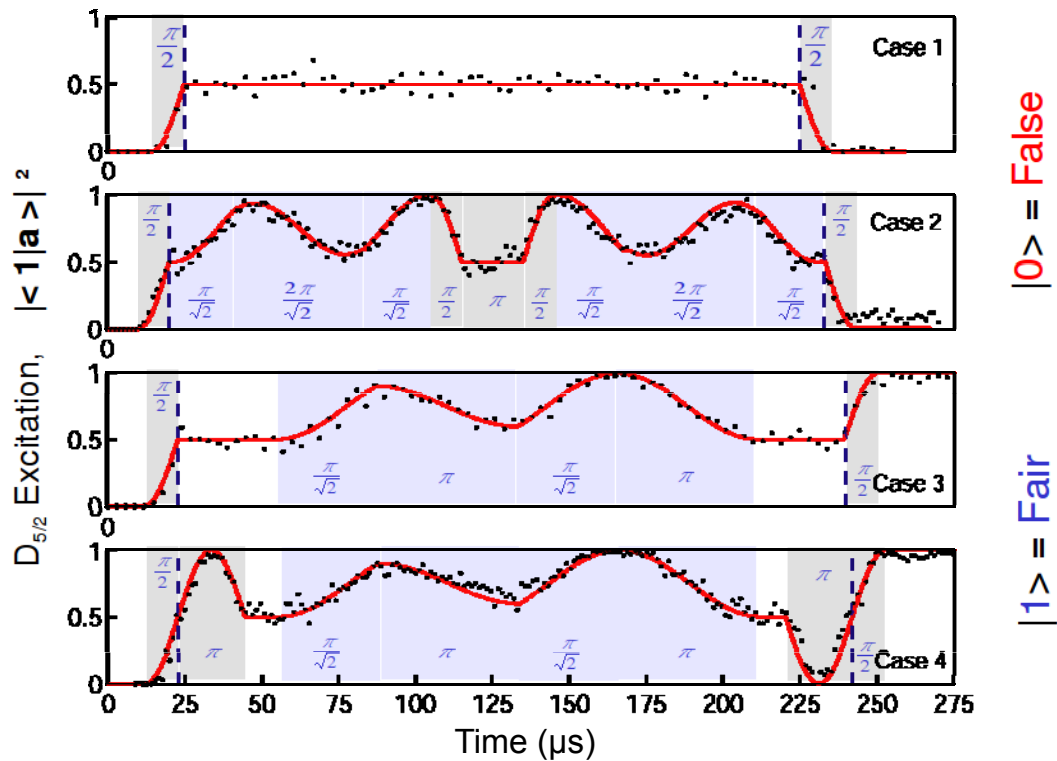
Deutsch Jozsa: Realization



Deutsch Jozsa: Realization



Deutsch Jozsa: Realization



Deutsch Jozsa: **Result**

	Constant		Balanced	
	Case 1	Case 2	Case 3	Case 4
expected $\langle 1/a \rangle^2$	0	0	1	1
measured $\langle 1/a \rangle^2$	0.019(6)	0.087(6)	0.975(4)	0.975(2)
expected $\langle 1/w \rangle^2$	1	1	1	1
measured $\langle 1/w \rangle^2$	--	0.90(1)	0.931(9)	0.986(4)

S. Gulde et al., Nature 412, 48 (2003)



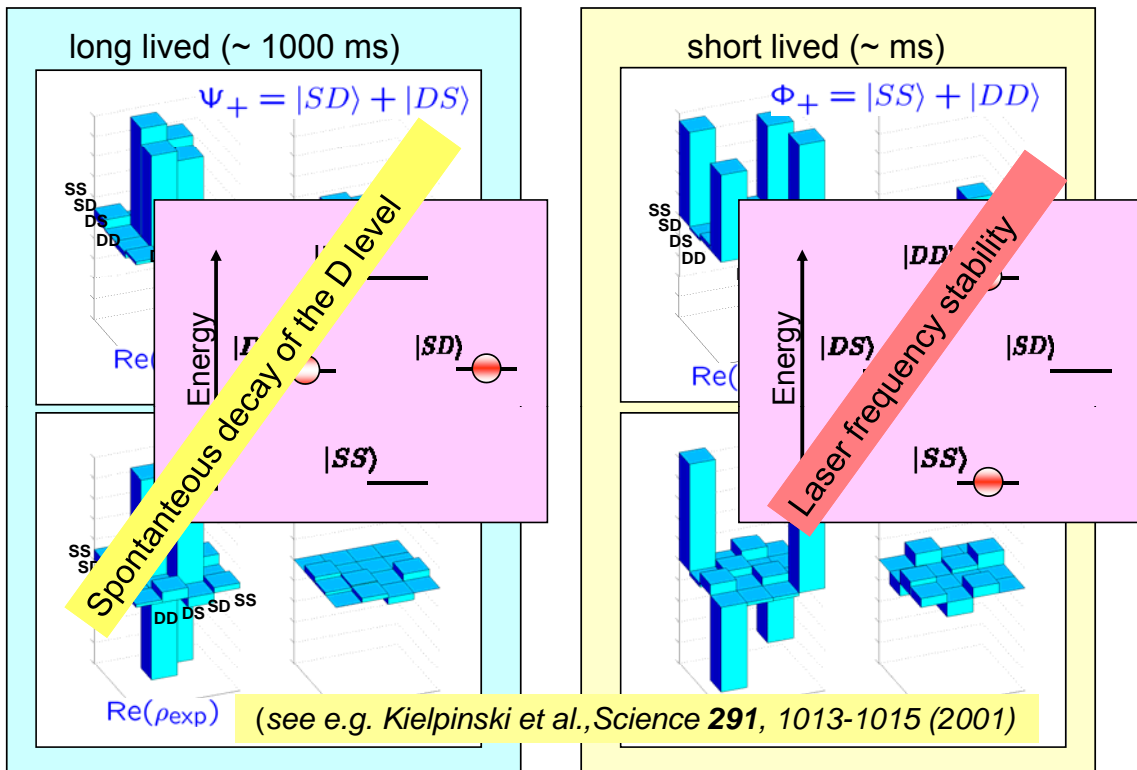
Conclusions

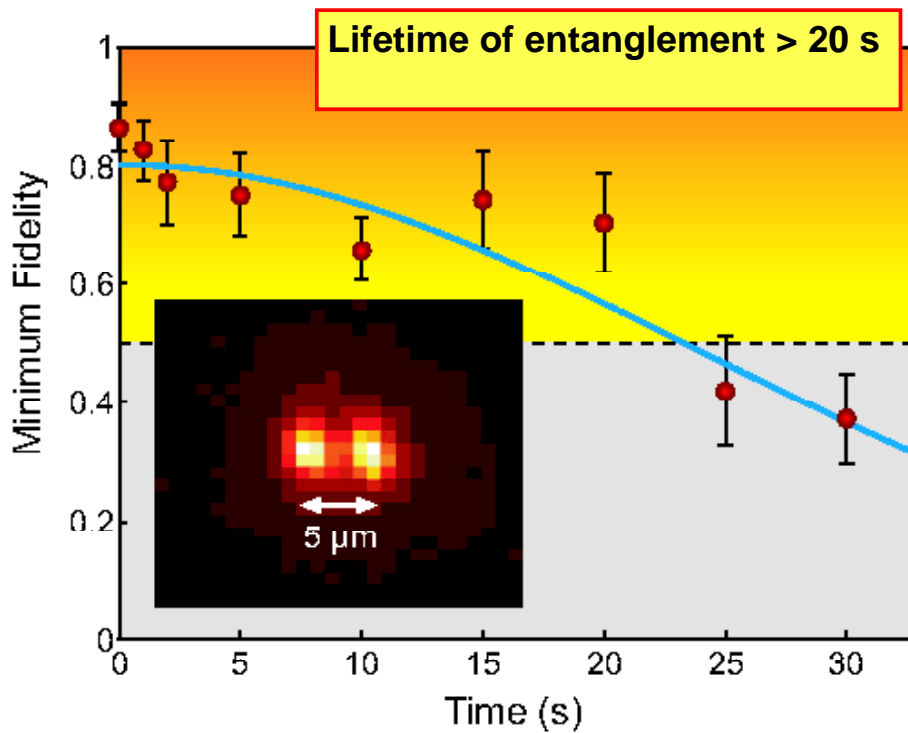
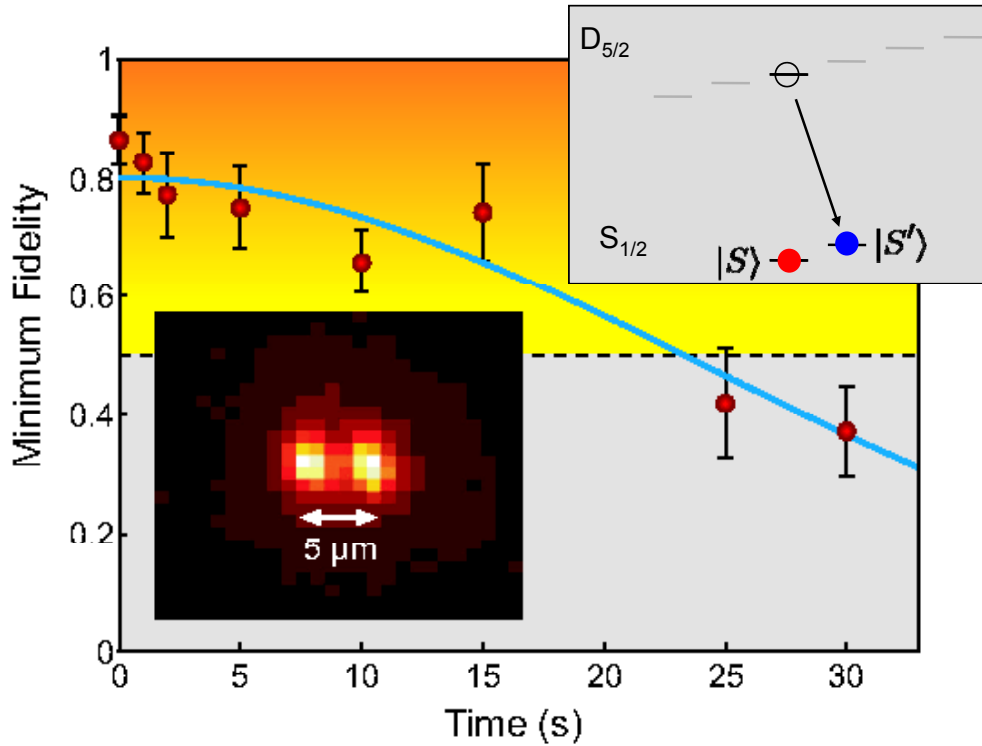


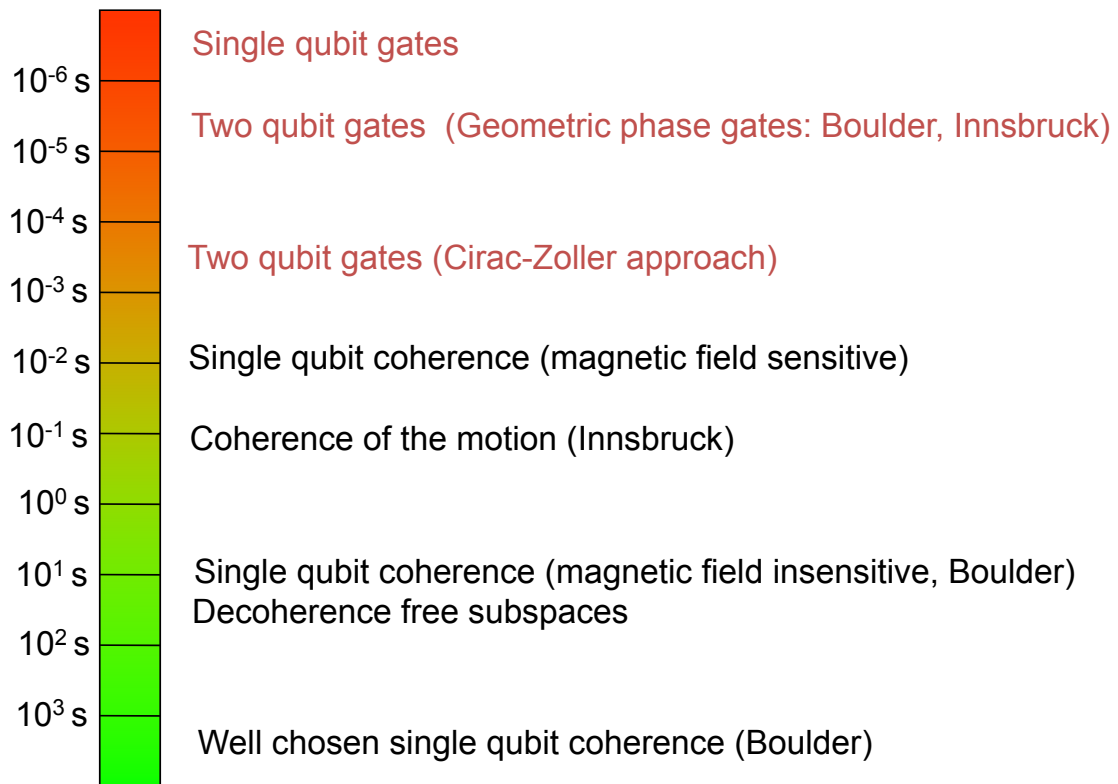
- Basics of ion trap quantum computing
- Measuring a density matrix
- Quantum gates
- Deutsch Algorithm



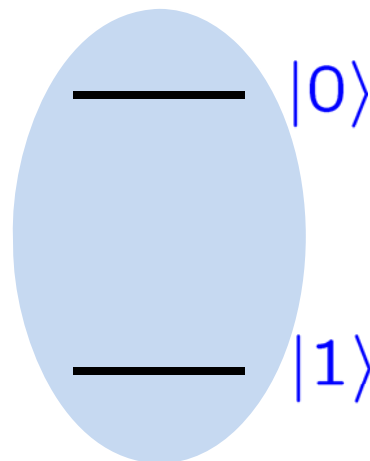
Berkeley, Nov 25th 2008

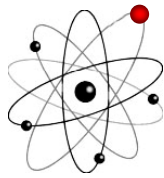




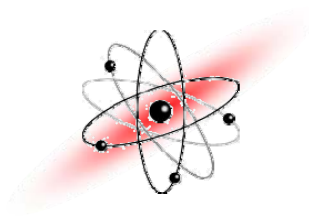


Two level system:

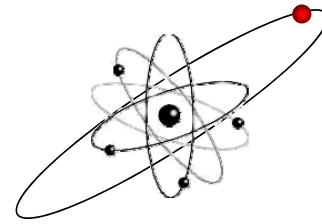




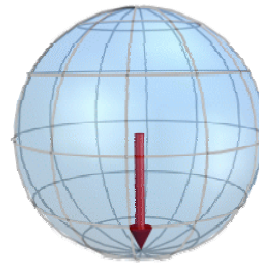
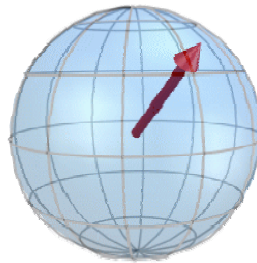
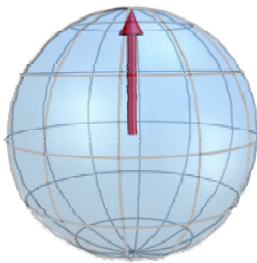
$$|0\rangle$$



$$\alpha|0\rangle + \beta|1\rangle$$



$$|1\rangle$$



Physical Qubit



Logical Qubit

$$|0\rangle_P = |D\rangle$$

$$|0\rangle_L = |SD\rangle$$

$$|1\rangle_P = |S\rangle$$

$$|1\rangle_L = |DS\rangle$$

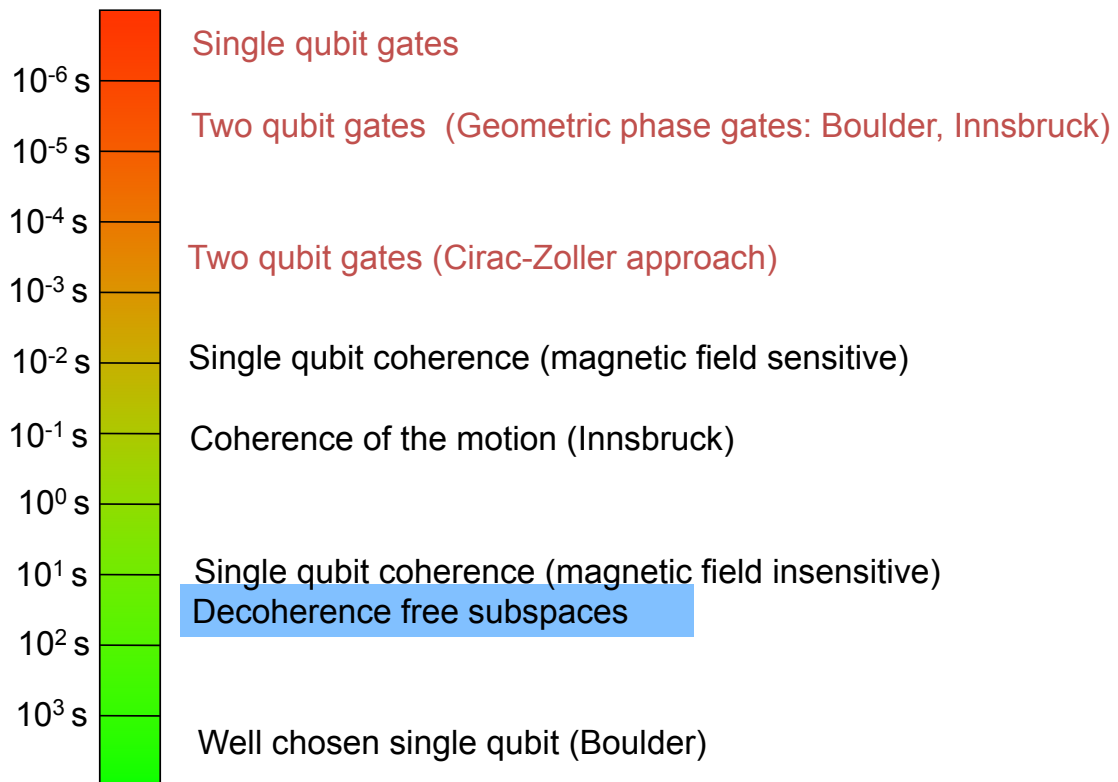
Effect of magnetic field or laser frequency fluctuations on qubits

$$\begin{array}{c}
 |D\rangle + |S\rangle \\
 \downarrow \\
 e^{i\phi}(|D\rangle + |S\rangle)
 \end{array}$$

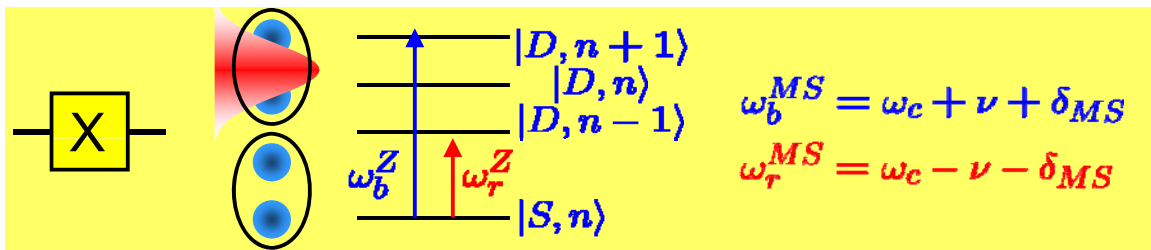
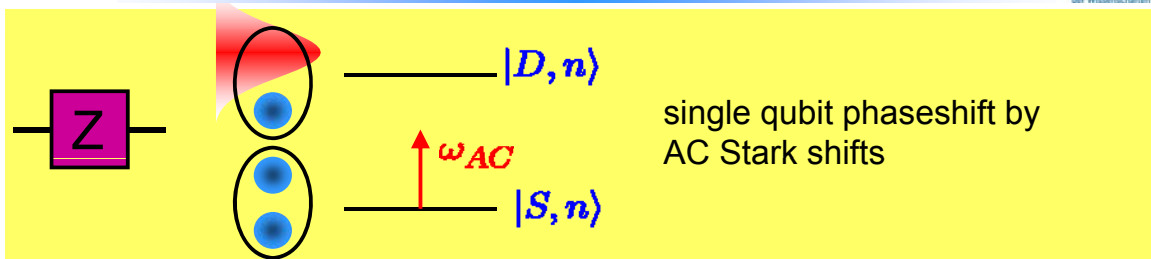
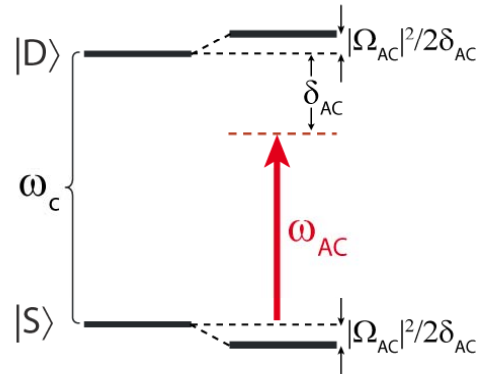
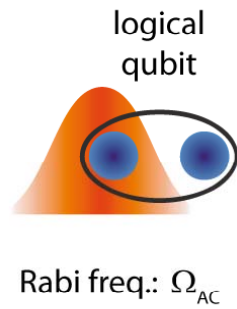


$$\begin{array}{c}
 |SD\rangle + |DS\rangle \\
 \downarrow \\
 e^{i\phi}(|SD\rangle + |DS\rangle)
 \end{array}$$

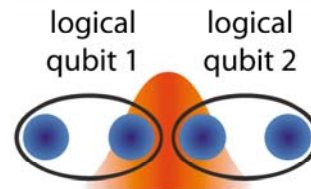
Logical qubit experiences global phase only



- single qubit operations
 - Z gates
 - X gates
- two –qubit operations
 - phase gate



Two body interactions preferred:

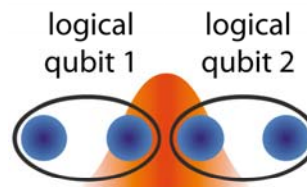


Most interactions cause the state to leave the decoherence free subspace.

Some solutions: [L. Aolita et al., PRA 75 052337 \(2007\)](#)

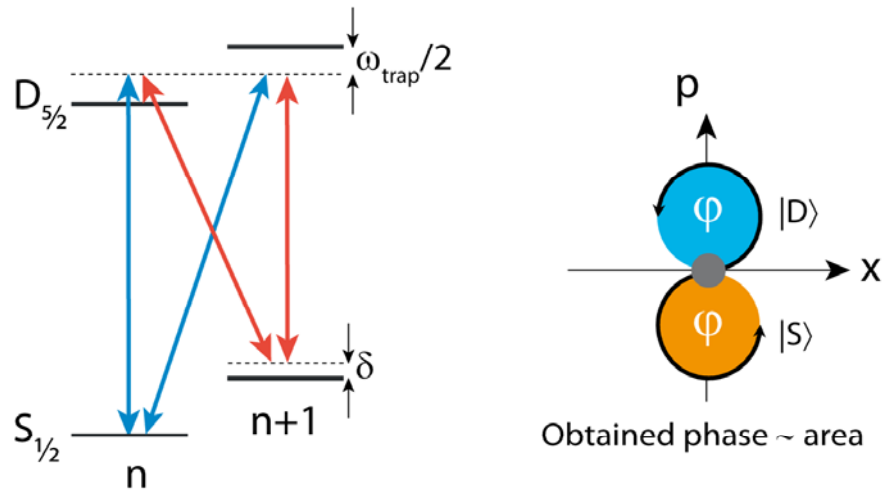
Action of the phase gate on two physical qubits:

$$\begin{array}{l}
 |DD\rangle \\
 |DS\rangle \\
 |SD\rangle \\
 |SS\rangle
 \end{array}
 \Rightarrow
 \begin{array}{l}
 e^{i\phi}|DD\rangle \\
 |DS\rangle \\
 |SD\rangle \\
 e^{i\phi}|SS\rangle
 \end{array}$$



...and on the logical qubits:

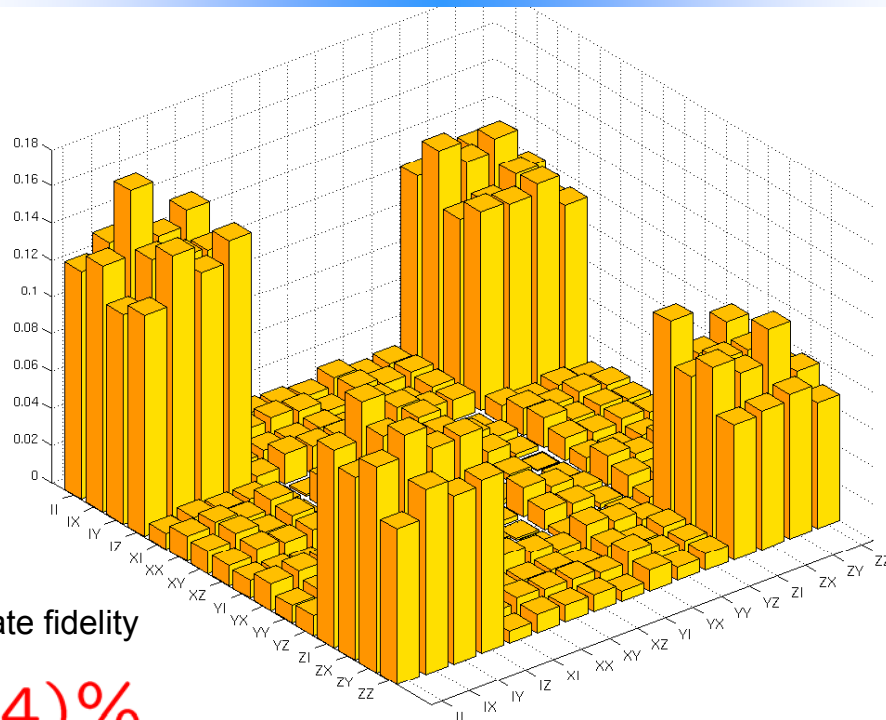
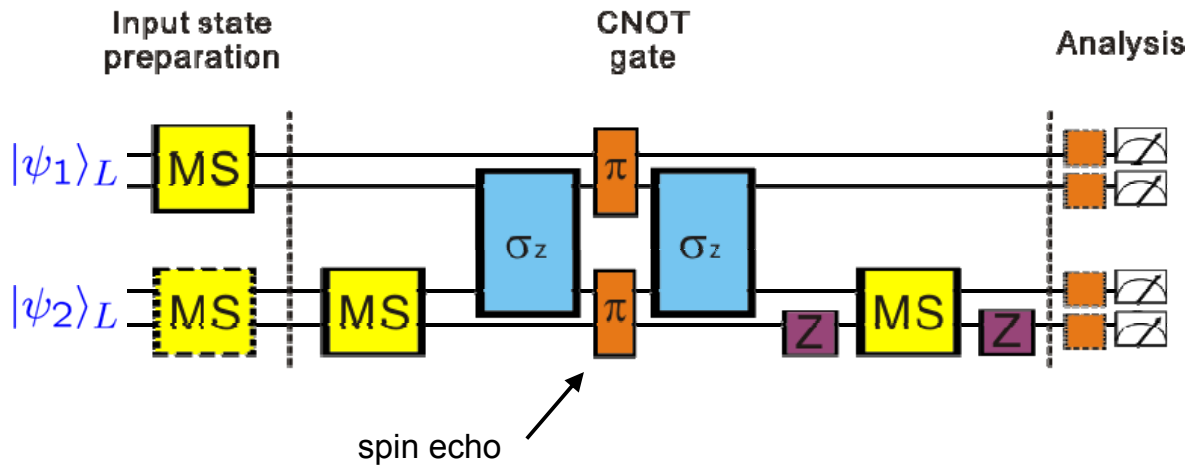
$$\begin{array}{l}
 |00\rangle_l \\
 |01\rangle_l \\
 |10\rangle_l \\
 |11\rangle_l
 \end{array}
 =
 \begin{array}{l}
 |S\rangle|DS\rangle|D\rangle \\
 |S\rangle|DD\rangle|S\rangle \\
 |D\rangle|SS\rangle|D\rangle \\
 |D\rangle|SD\rangle|S\rangle
 \end{array}
 \Rightarrow
 \begin{array}{l}
 |S\rangle|DS\rangle|D\rangle \\
 |S\rangle e^{i\phi}|DD\rangle|S\rangle \\
 |D\rangle e^{i\phi}|SS\rangle|D\rangle \\
 |D\rangle|SD\rangle|S\rangle
 \end{array}
 =
 \begin{array}{l}
 |00\rangle_l \\
 e^{i\phi}|01\rangle_l \\
 e^{i\phi}|10\rangle_l \\
 |11\rangle_l
 \end{array}$$



D. Leibfried, et al., Nature **422** 412 (2003)

K. Kim et. al., Phys. Rev. A **77**, 050303 (2008)

			<p>single qubit phaseshift by AC Stark shifts</p>
			$\omega_b^{MS} = \omega_c + \nu + \delta_{MS}$ $\omega_r^{MS} = \omega_c - \nu - \delta_{MS}$
			$\omega_b^Z = \omega_c + \nu/2 + \delta_z$ $\omega_r^Z = \omega_c - \nu/2 - \delta_z$



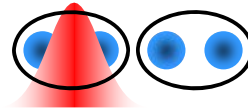
mean gate fidelity

89(4)%

mean gate fidelity: 89(4)%
(after DFS postselection)

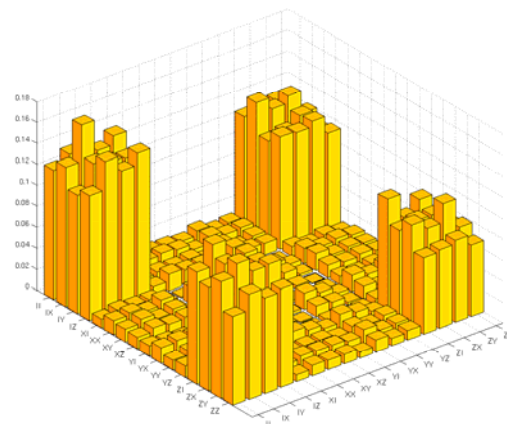
Main limitations:

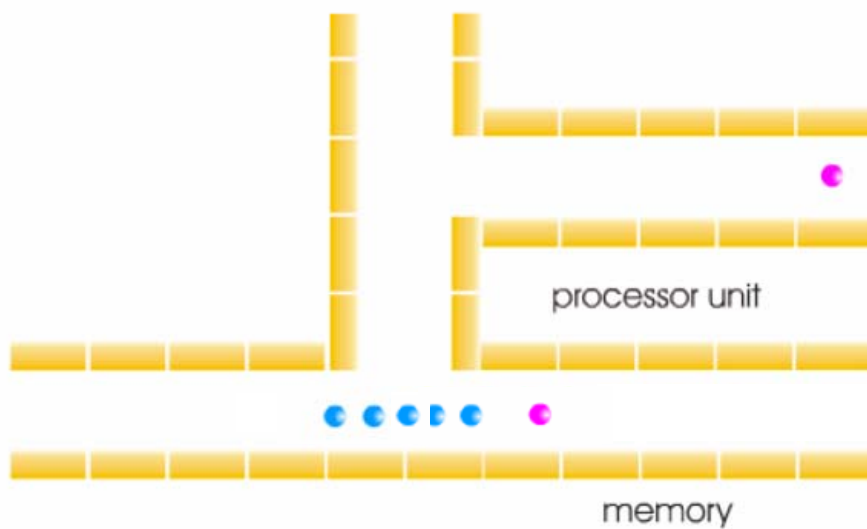
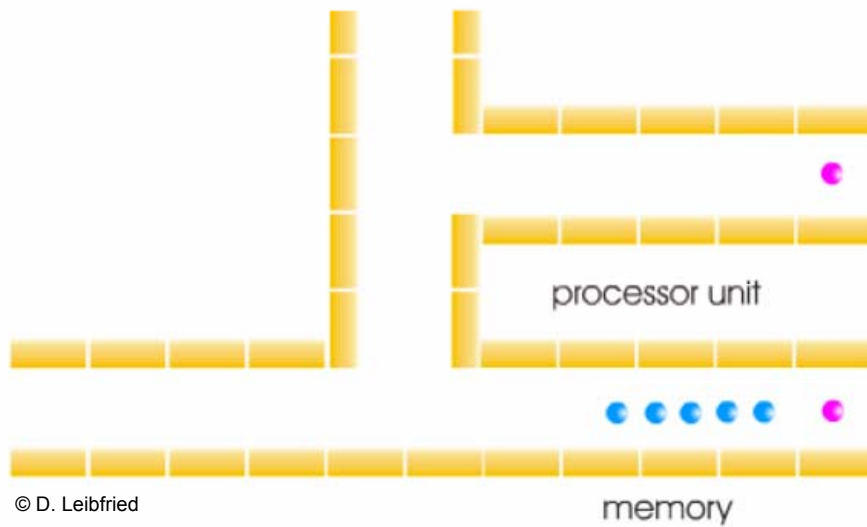
- spurious laser frequency components
- off-resonant coupling to other levels
- intensity stability on ions
- addressing errors

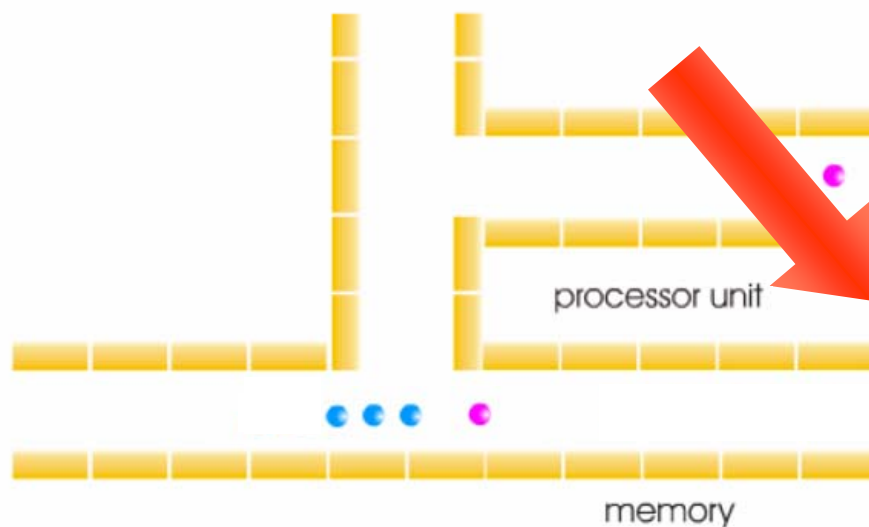
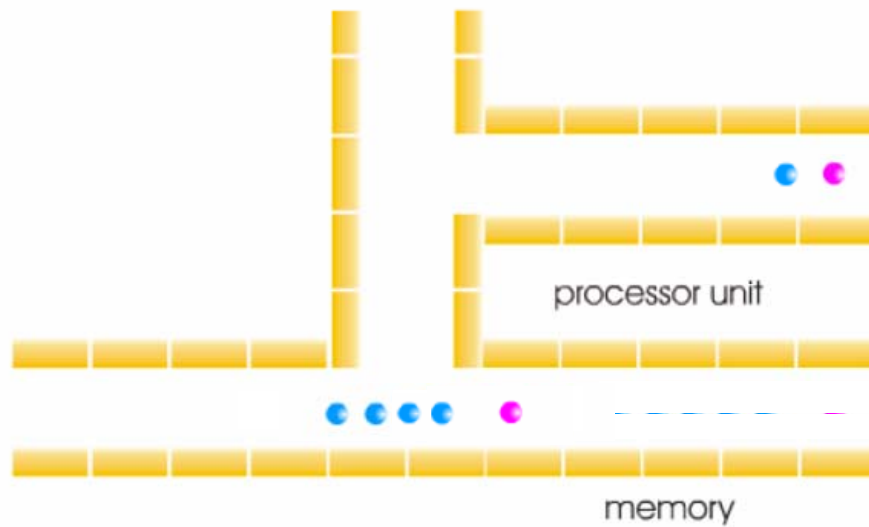


Advantages:

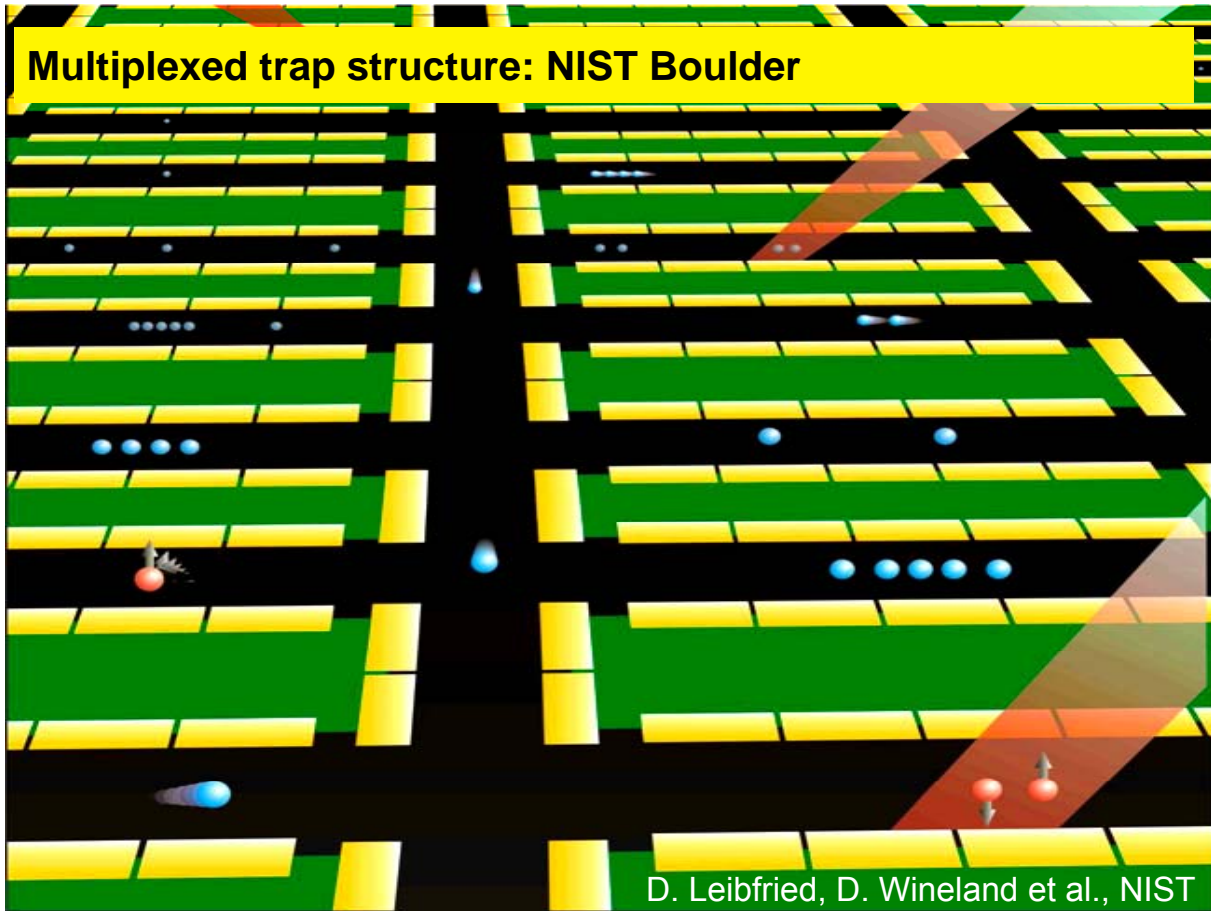
- lifetime limited coherence time
- insensitive to laser linewidth
- insensitive to AC-Stark shifts







Multiplexed trap structure: NIST Boulder

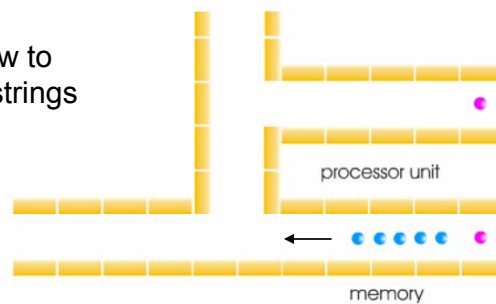


D. Leibfried, D. Wineland et al., NIST

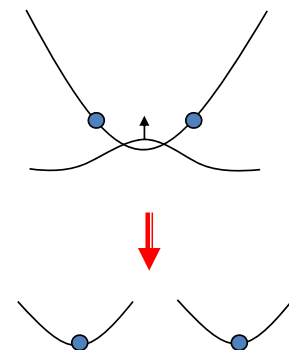
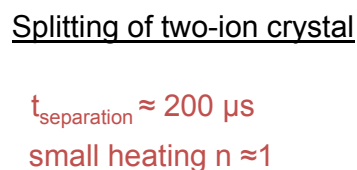
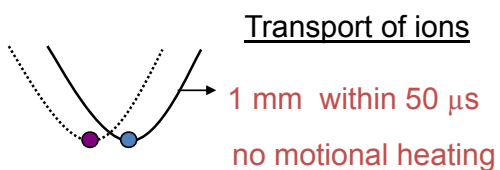
Segmented ion traps as scalable trap architecture

(ideas pioneered by D. Wineland, NIST)

Segmented trap electrode allow to transport ions and to split ion strings



State of the art:



„Architecture for a large-scale ion-trap quantum computer“, D. Kielpinski et al, Nature **417**, 709 (2002)

„Transport of quantum states“, M. Rowe et al, quant-ph/0205084

Scaling of this approach?

Problems :

- Coupling strength between internal and motional states of a N-ion string decreases as

$$\eta \propto \frac{1}{\sqrt{N}}$$

(momentum transfer from photon to ion string becomes more difficult)

-> Gate operation speed slows down

- More vibrational modes increase risk of spurious excitation of unwanted modes
- Distance between neighbouring ions decreases -> addressing more difficult

-> Use flexible trap potentials to split long ion string into smaller segments and perform operations on these smaller strings